

An aerial view of a large, modern train station with multiple tracks and high-speed trains. The trains are blue and yellow, and the station has a complex, multi-level structure with white pillars and a glass roof. The text is overlaid on a blue rectangular background in the center of the image.

An Agent-Based Approach to Modelling Public Transport Dynamics

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Outline

Concepts

1. PT assignment principles
2. Modelling PT dynamics
3. Agent-based simulation model

Applications

1. Congestion
2. Real-time travel information
3. Service disruptions
4. Control and operational strategies

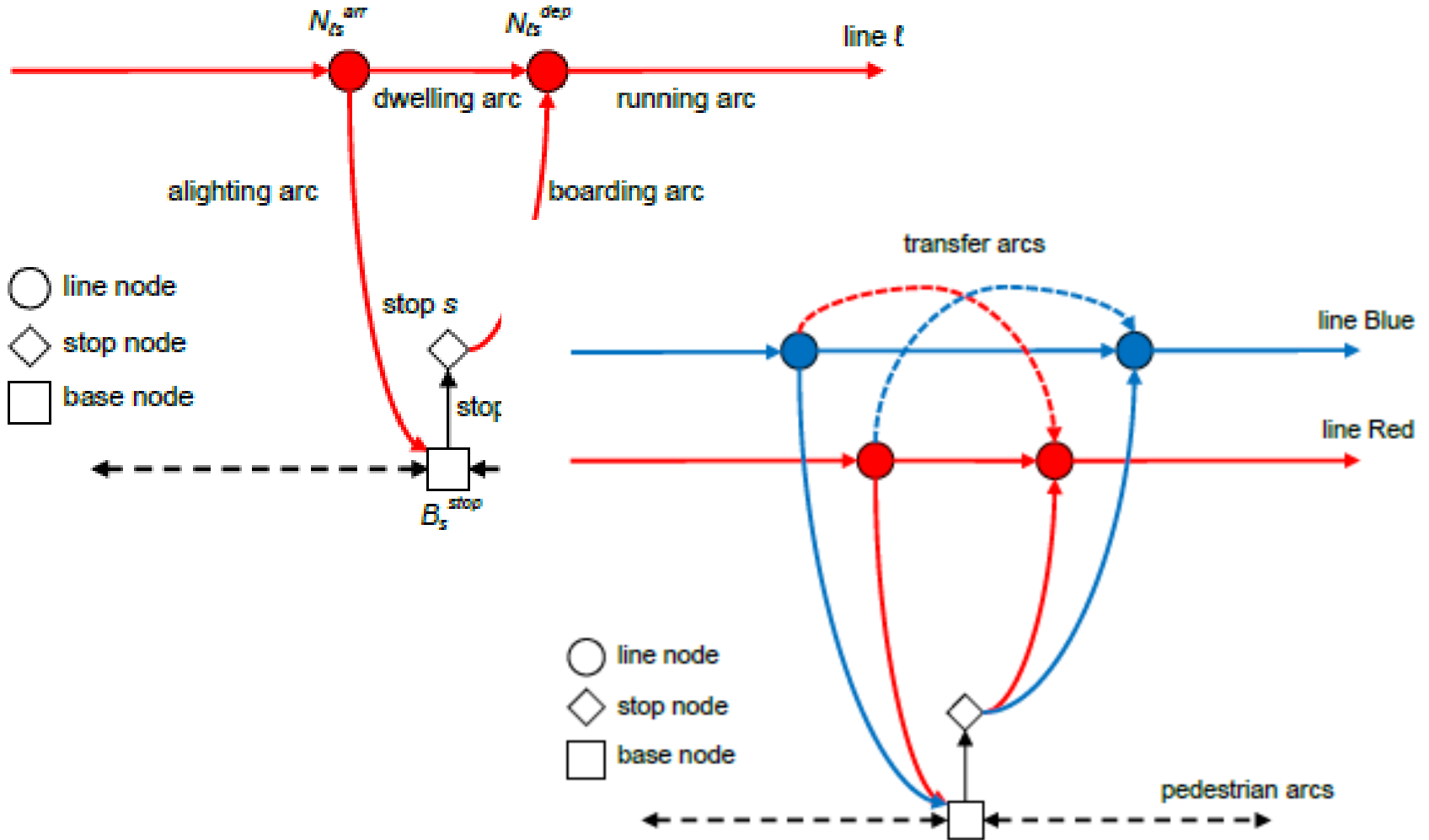


PTA principles and approaches

Frequency-based: Assignment principles

- PT network is represented in terms of segments of **lines**
- Demand is assigned based on service **frequencies**
- Adopting concepts and solution methods from car traffic assignment

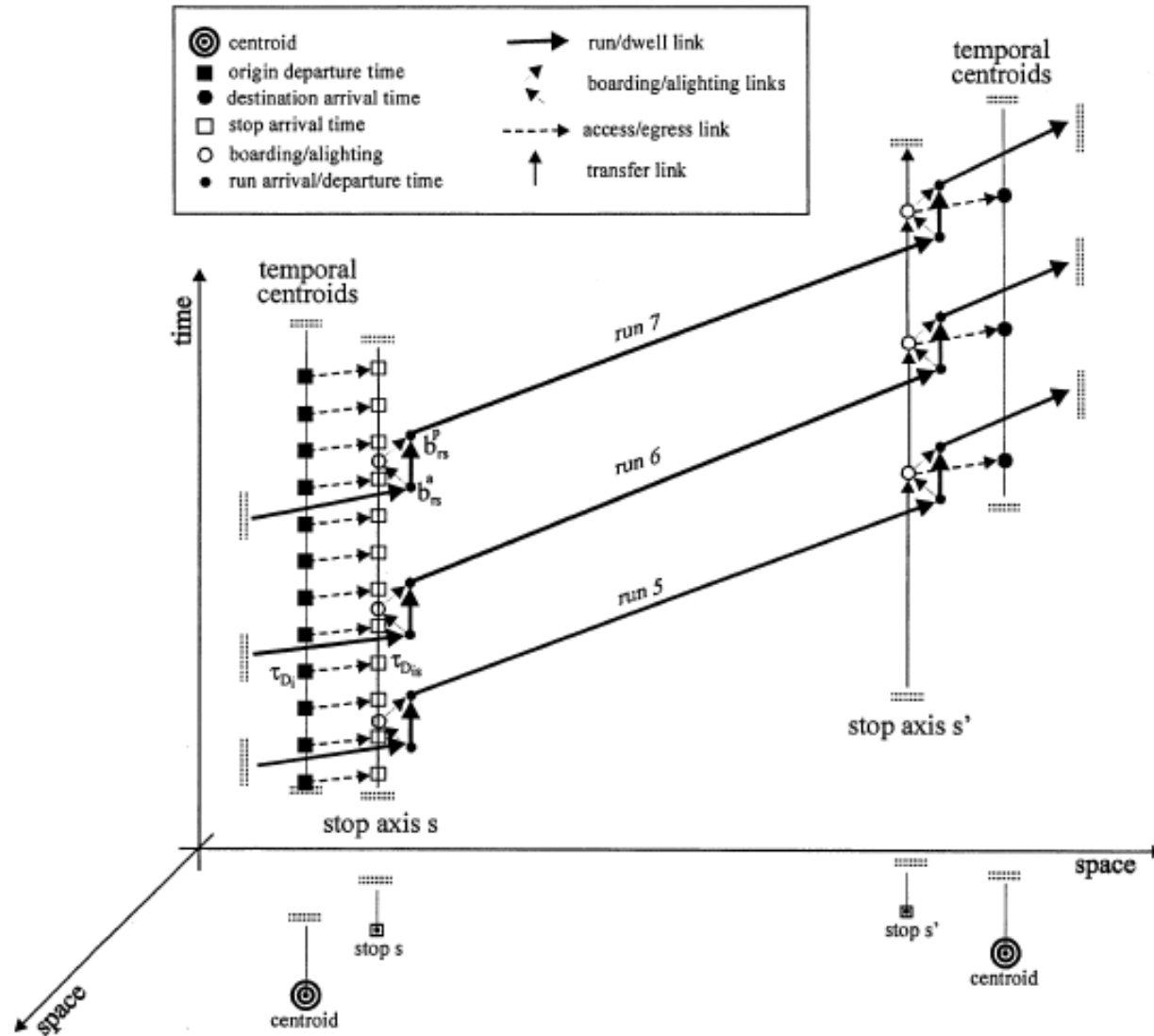
Frequency-based: Network representation



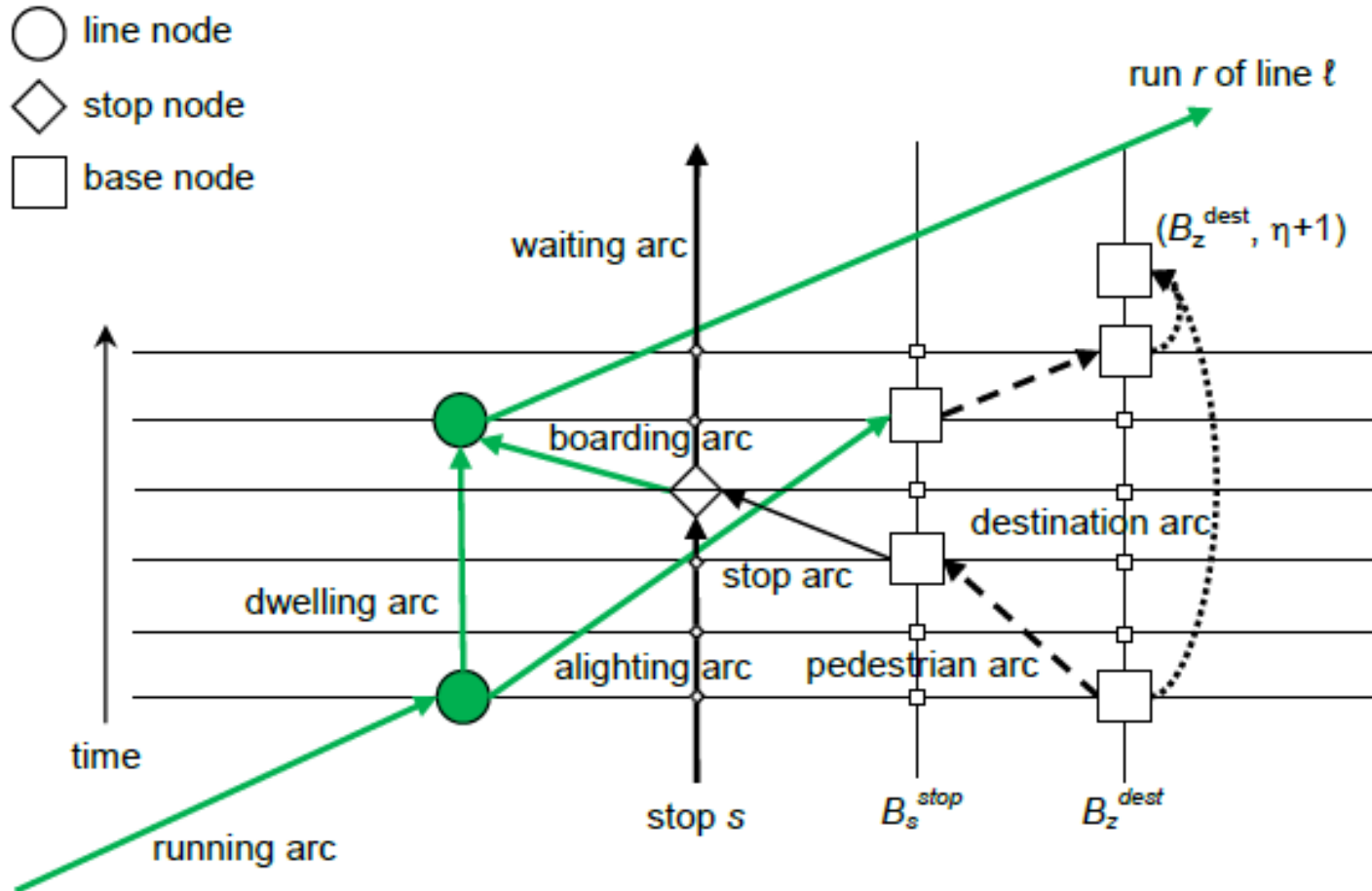
Schedule-based: Assignment principles

- PT network is represented in terms of individual **vehicle trips/runs** following a timetable
- Demand is assigned to specific trips, takes into account **time-dependent** characteristics
- The concept of accumulative shortest path is not valid anymore

Schedule-based: Network representation



Schedule-based: Stop topology



Traditional assumptions

- Travel times is equal on all lines riding the same arc (FB)
- Passengers arrive randomly at stops
- No capacity constraints
- Perfect reliability (regularity – FB; punctuality – SB)
- Passengers board the first arriving vehicle
- Perfect information
- Homogenous travellers' population

Flow-dependent in-vehicle time

Flow-capacity ratio multiplier

- Already in the original presentation of optimal strategies
- on-board crowding
- Link travel time as a non-linear function of passenger flows
- Iterative network loading to obtain equilibrium
- BPR crowding function

$$\gamma_{ls}(q_a) = 1 + \alpha_\ell^{run} \cdot \left(\frac{q_a}{f_{ls} \cdot \kappa_\ell^{veh}} \right)^{\beta_\ell^{run}}, \quad a = (N_{ls}^{dep}, N_{ls+\ell}^{arr}) \in A^{run}$$

- $q_a / (f_{ls} \cdot \kappa_\ell^{veh})$ is the saturation rate of the vehicle on the line segment;
- α_ℓ^{run} and β_ℓ^{run} are the BPR coefficient and exponent for running congestion.

Flow-dependent travel time

Effective frequency

- Assigning weights to waiting times
- Reliability effects and risk of denied boarding
- An infinite penalty when capacity is exceeded
- Reducing the nominal frequency by the BPR term

$$f_{ls}^{eff}(q_a) = \frac{f_{ls}}{1 + \alpha_\ell^{wait} \cdot \left(\frac{q_a}{f_{ls} \cdot \kappa_\ell^{veh}} \right)^{\beta_\ell^{wait}}}, \quad a = (N_{ls}^{dep}, N_{ls+\ell}^{arr}) \in A^{run}$$

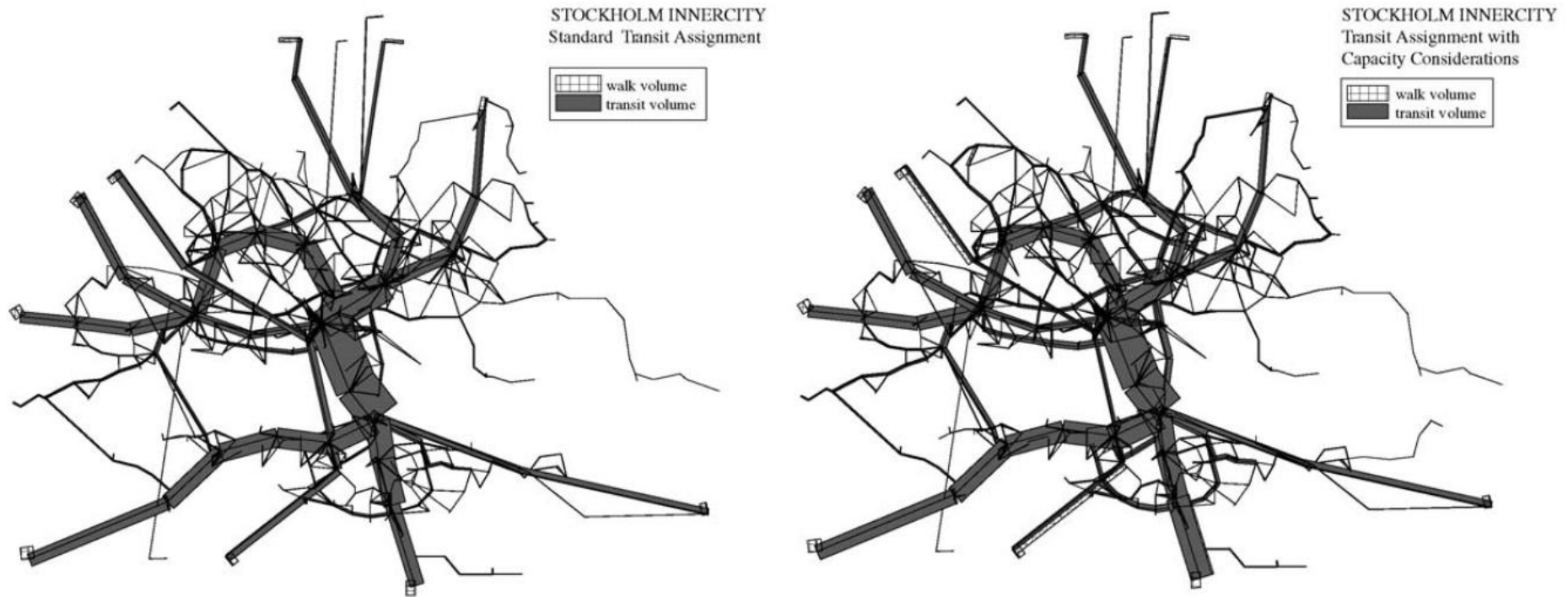
$$t_{ls}^{wait}(q_a) = \frac{0.5}{f_{ls}^{eff}(q_a)} \cdot (1 + \sigma_{ls})$$

Does not guarantee that capacity is not exceeded!

Average VOC ratio drops from 4.77 to 1.5

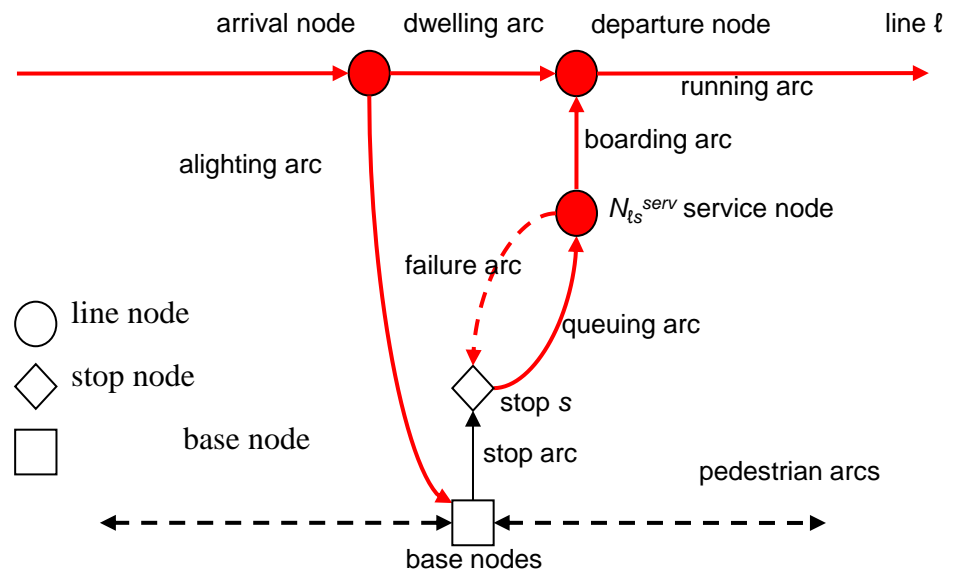
Number of over-saturated line segments drops from 45 to 10

Cpeda et al. (2006)



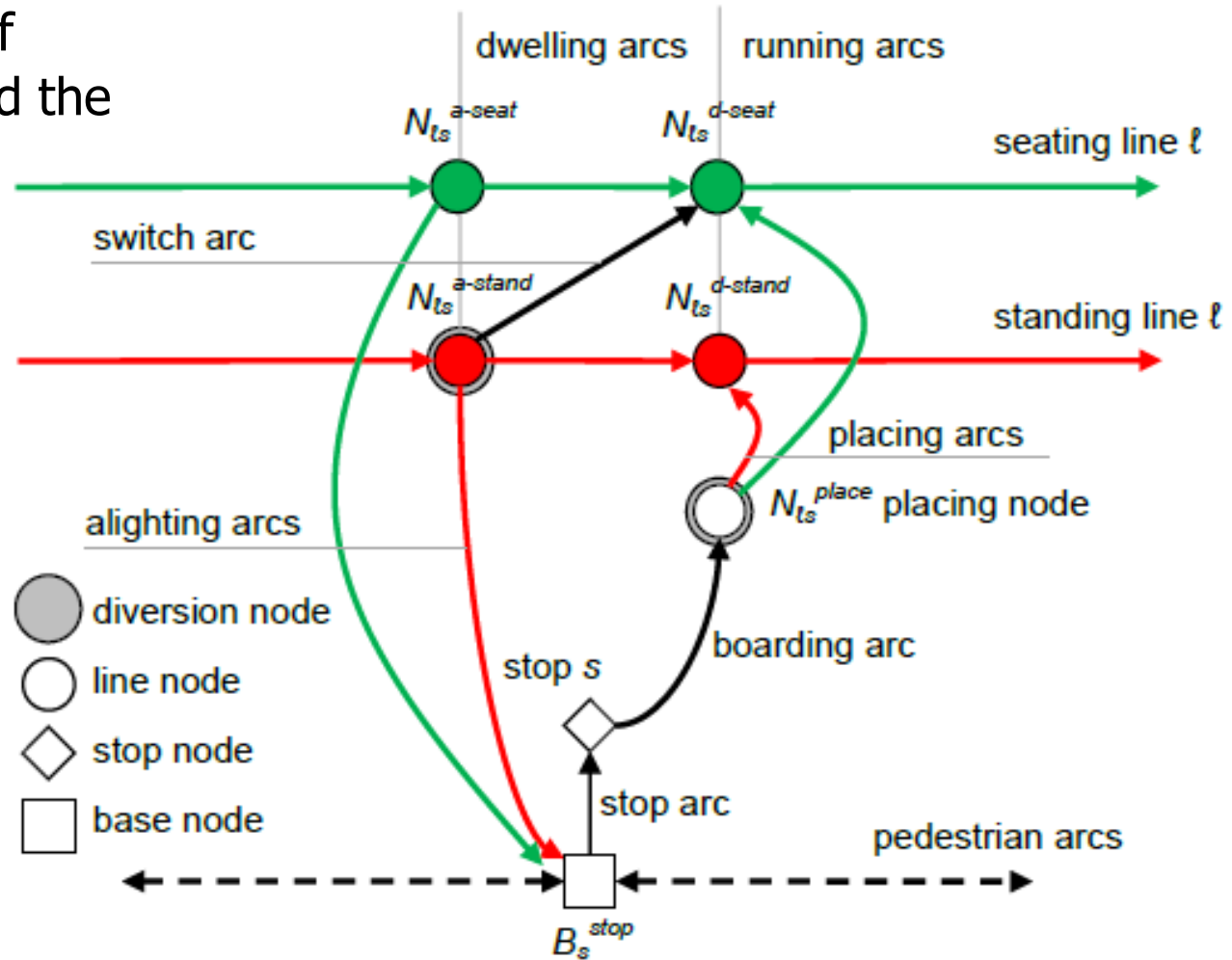
Failure-to-board probability

- FB: a quasi-dynamic model where *the share of passengers that exceeds the residual capacity* on the respective time period is transmitted to the next period
- SB: guarantees that capacity constraints are *satisfied at the individual vehicle level* by introducing new arcs between successive vehicle trips
- Queuing (FIFO, mingling)



Seating and priorities

- satisfy the set of priority rules and the seat capacity constraint



Main trends in developments of PT assignment models (Liu et al 2010)

- Consistently lagged behind developments in traffic modeling
- Expected and emerging developments
 - **Multi-agent** simulation models
 - **Dynamic** loading process
 - **Adaptive** user decisions
 - **Supply uncertainties**

2.

Agent-based approach to PTA

Prominent research questions

- How does the **system perform** under various conditions?
- How can APTS be deployed most **effectively** to improve service operations?
- How to **mitigate** and manage service **disruptions**?
- How could service providers and users become more **adaptive** by taking advantage of the abundance of real-time data?
- What is the **impact** of APTS measures?

Agent-based TAM

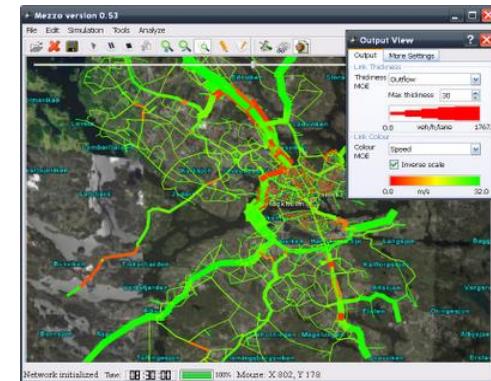
- Represents individual vehicles and travellers
- Emerging solution based on agents interaction with each other throughout the simulation
- En-route decisions
- Day-to-day learning as proxy to equilibrium conditions
- Integration with traffic simulation models



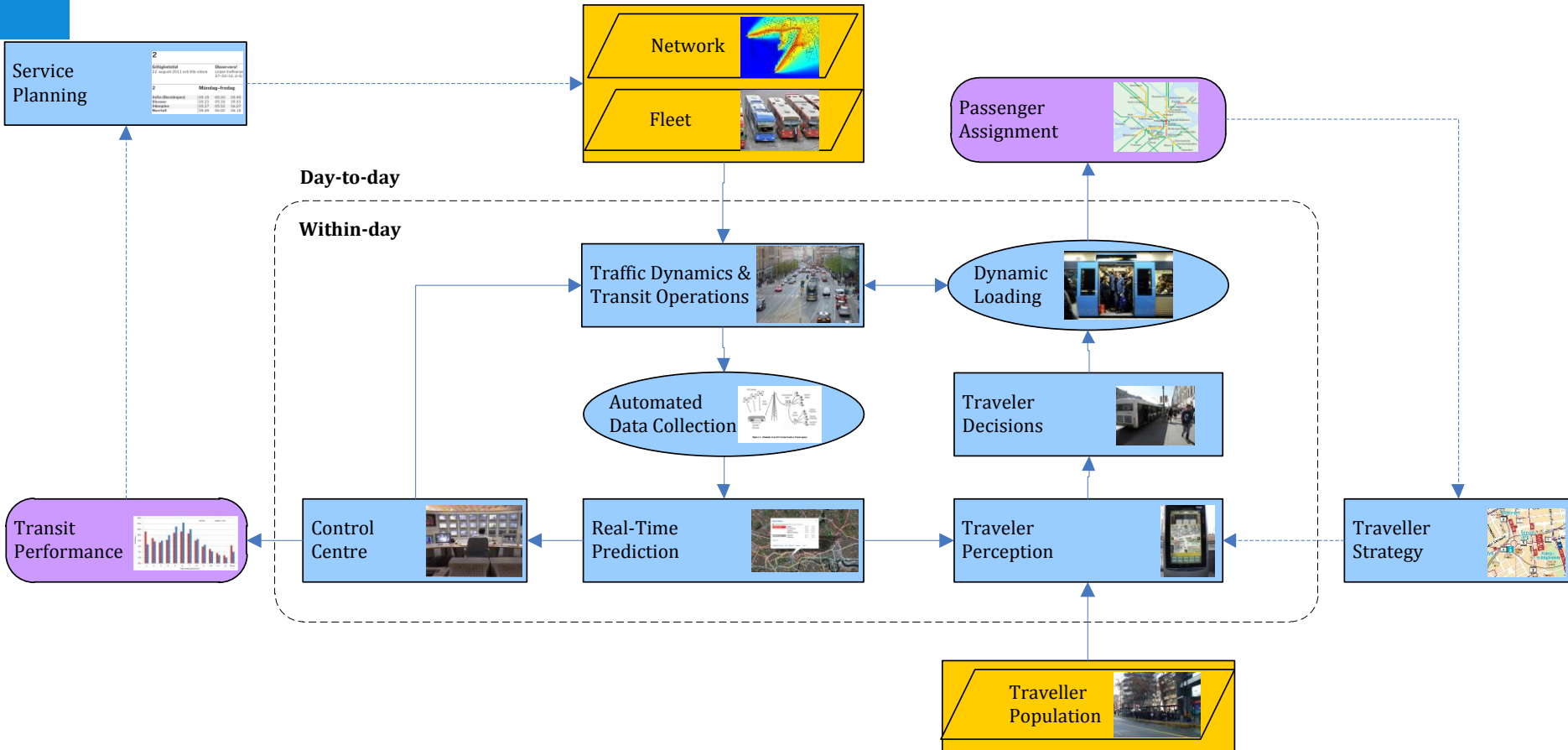
Implementation: BusMezzo

Transit Assignment and Operations Simulation Model

- A framework for analyzing transit performance under various operational conditions and APTS
- **BusMezzo**: integrated into Mezzo, a mesoscopic traffic simulation model
- Agent-based
- Operations-oriented
- Sources of uncertainty
- Adaptive decision making
- System level analysis



A modelling framework for Analyzing Public Transport Operations



Network representation



- *Transit vehicle trajectory*

- Ride
- Queue
- Dwell
- Recover

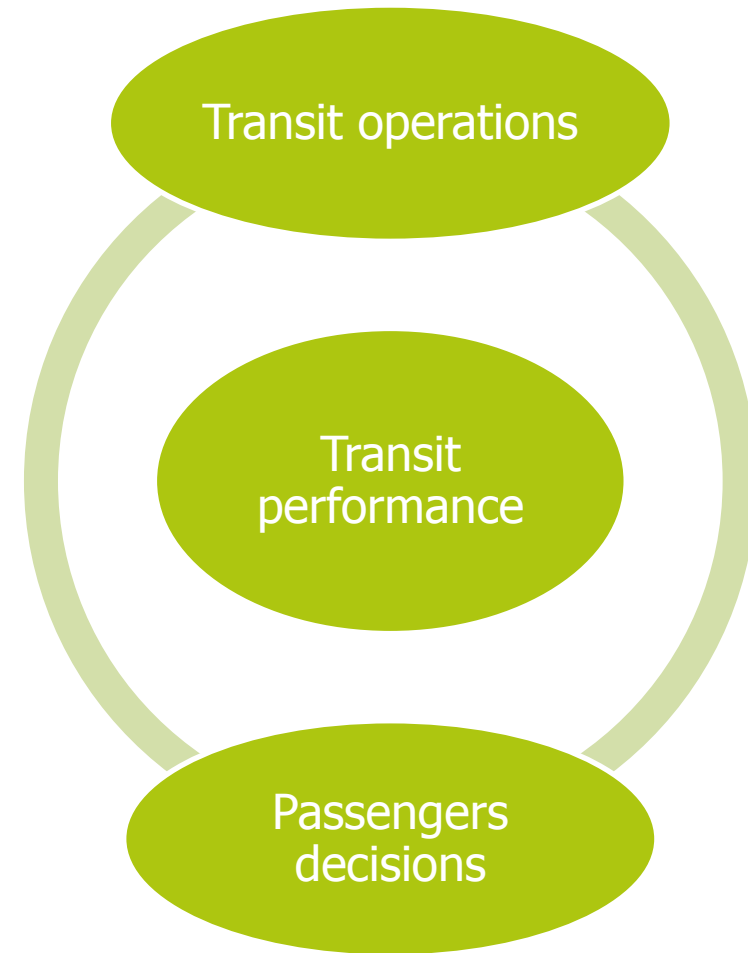
- *Traveller trajectory*

- Walk
- Wait
- On-board

Public Transport Dynamics

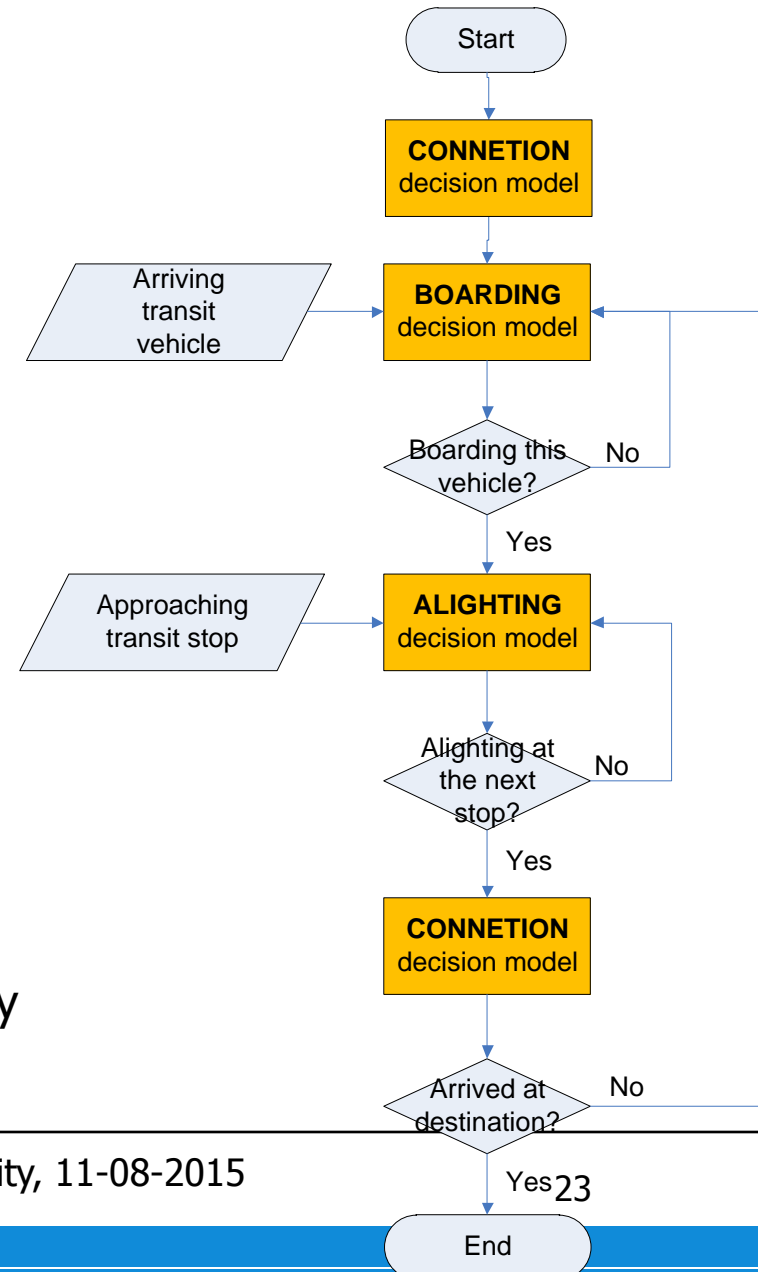
Joint car and PT; mode-specifics
Dwell times
Fleet; vehicle scheduling
Crowding and capacity

Operations planning
Control and management strategies
Adaptive route choice
Real-time information



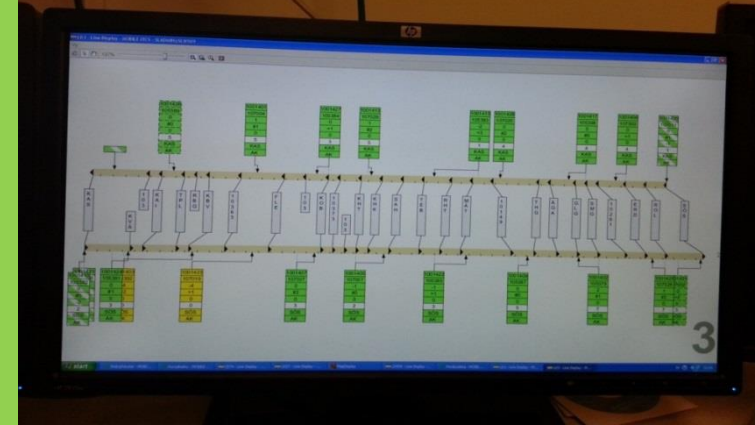
Demand representation

- $\lambda_{od}(t, \tau)$ – Poisson arrival process
- Non-compensatory rule-based choice-set generation process
- En-route decisions
 - Assess the attributes of each available path
$$v_{i,n} = \beta_{i,n} X_{i,n}$$
 - Calculate the *joint utility* of the bundled paths
$$v_{I,n} = \ln \sum_{i \in I} e^{v_{i,n}}$$
- Path: outcome of successive decisions
- Preserve passenger integrity from one day to the other



Applications

Reliability and
Control



Real-time
Information



Network
Resilience

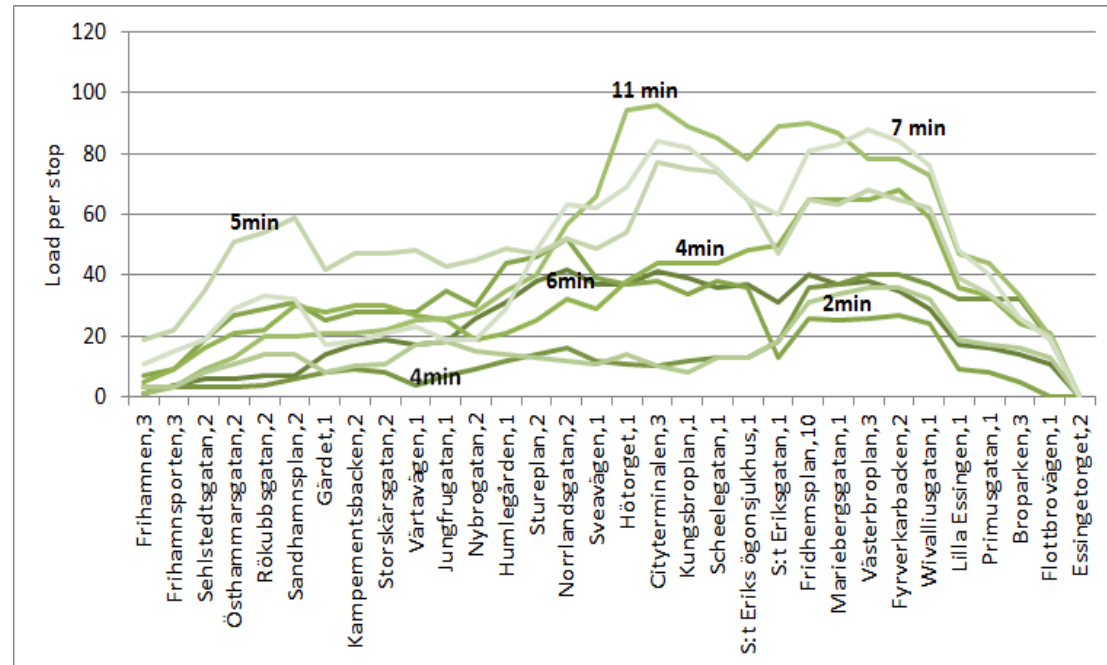
Congestion

Application: Increased capacity

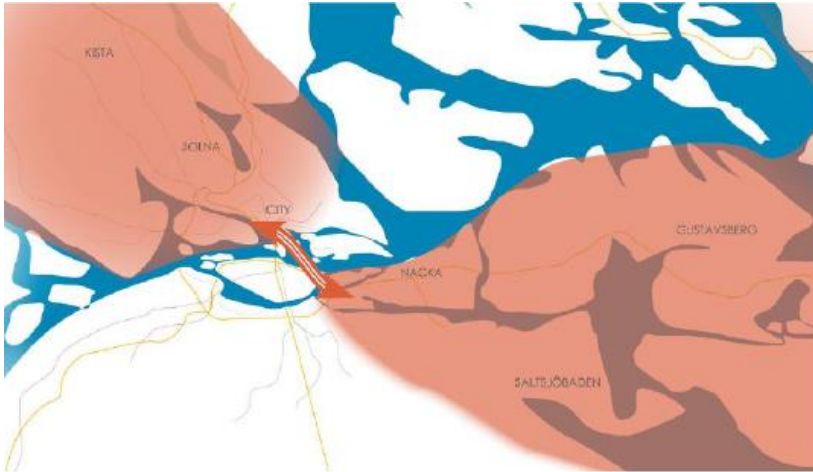


The dynamics of reliability & congestion

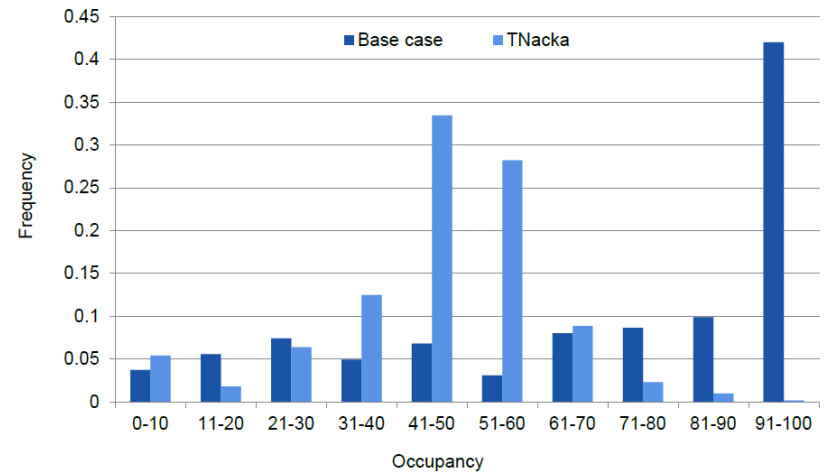
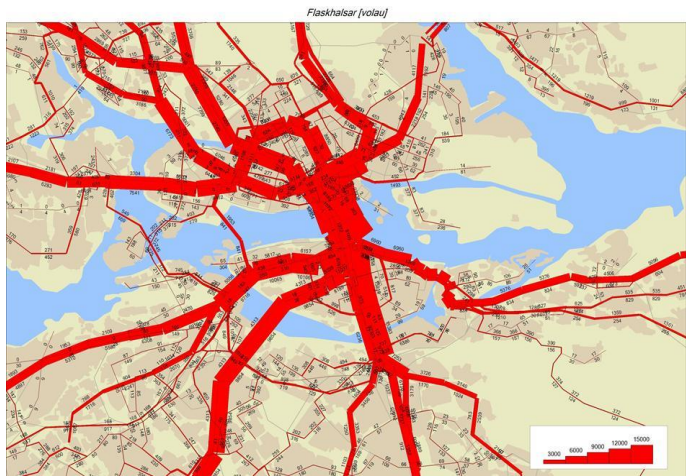
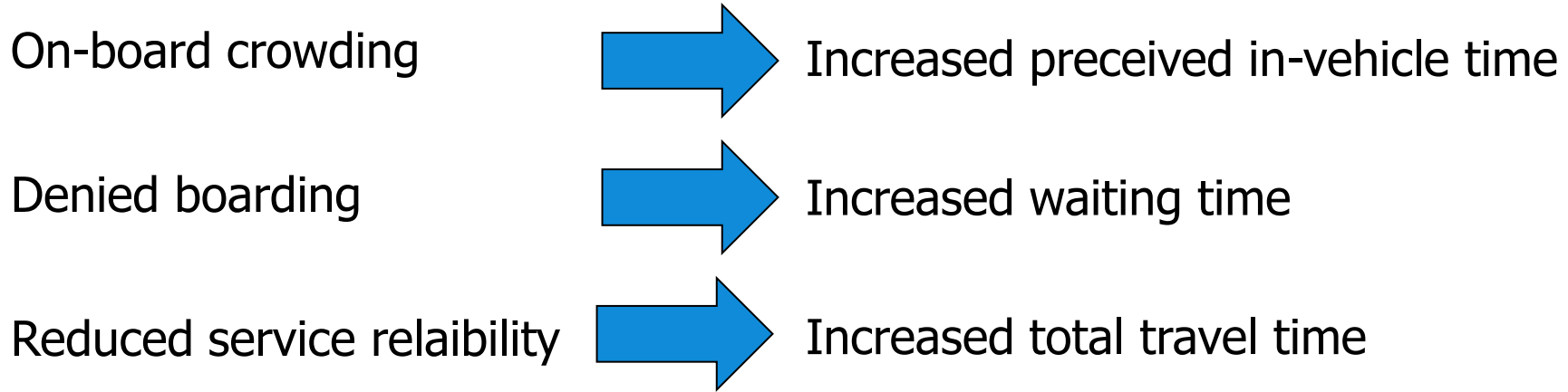
- Route choice
- Service reliability
- Demand variation



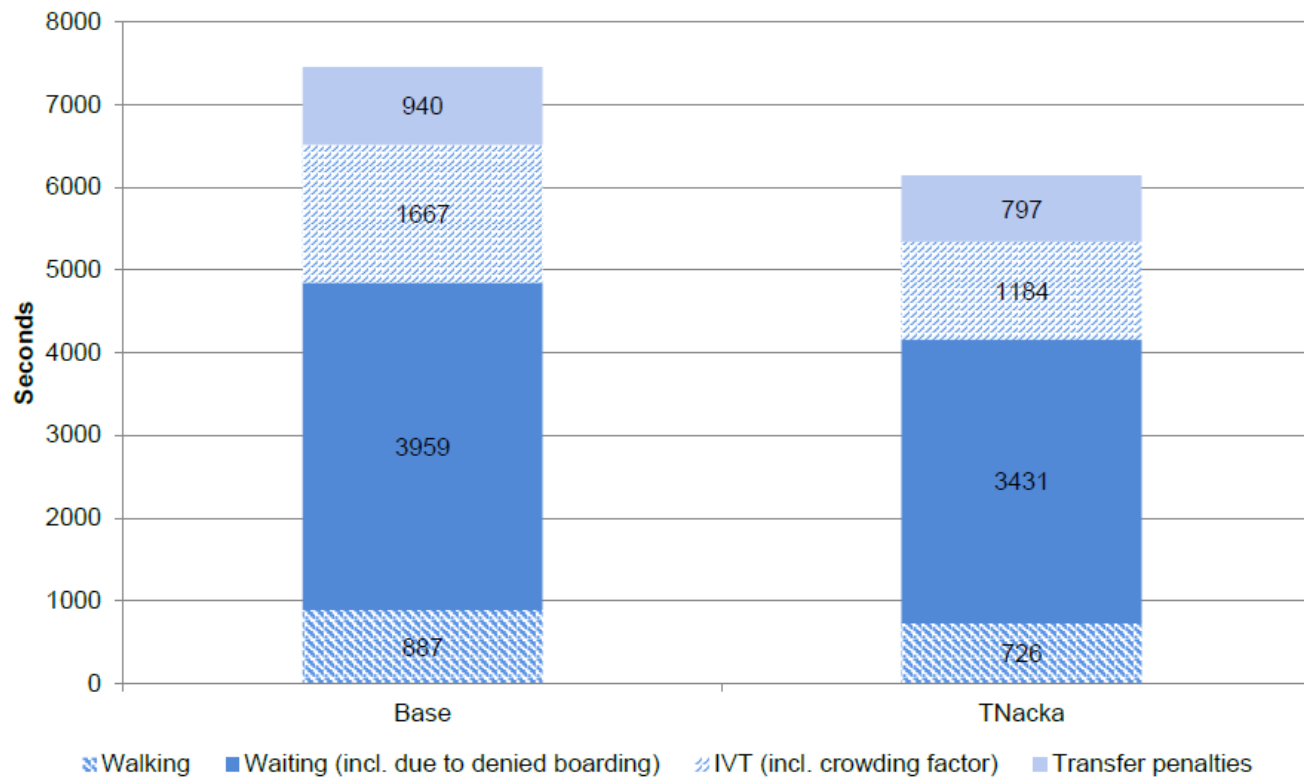
How can the value of reduced congestion be quantified?



Evaluation of congestion effects



Appraisal of Increased Capacity

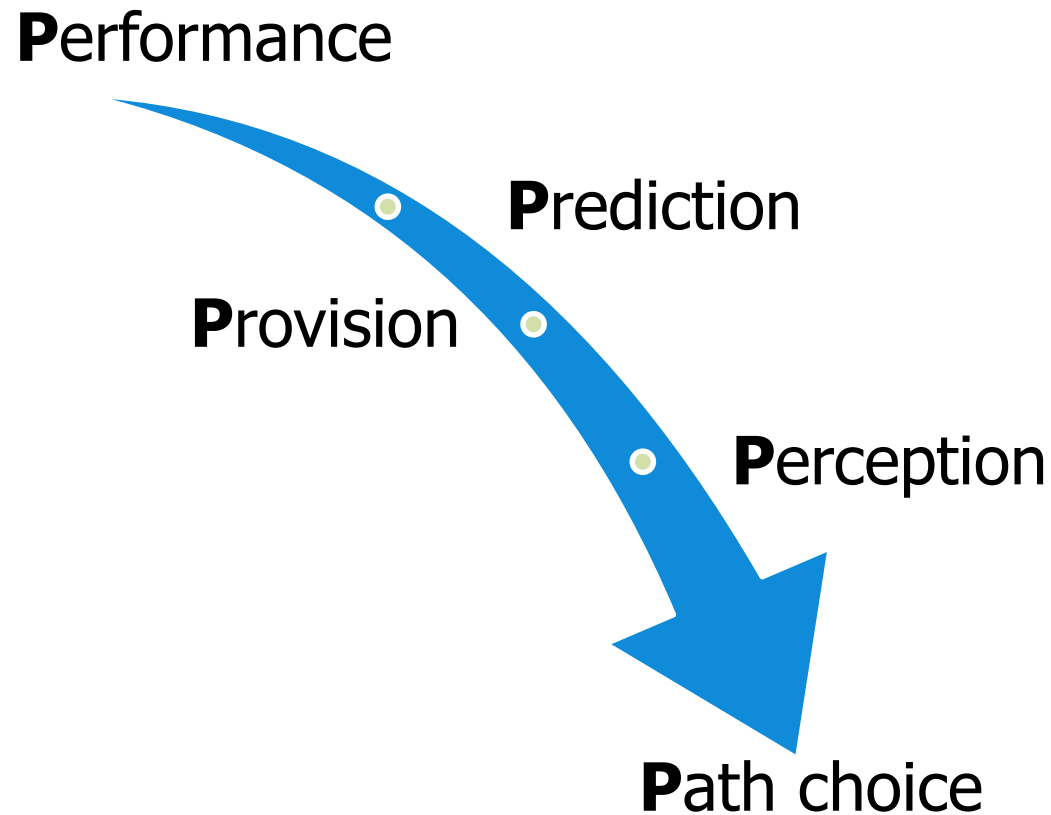


- Crowding factor in static/dynamic model: +3%/+60%
- Value of increased capacity: underestimated in static models
- Overestimation in BusMezzo: currently incorporate crowding in the route choice model

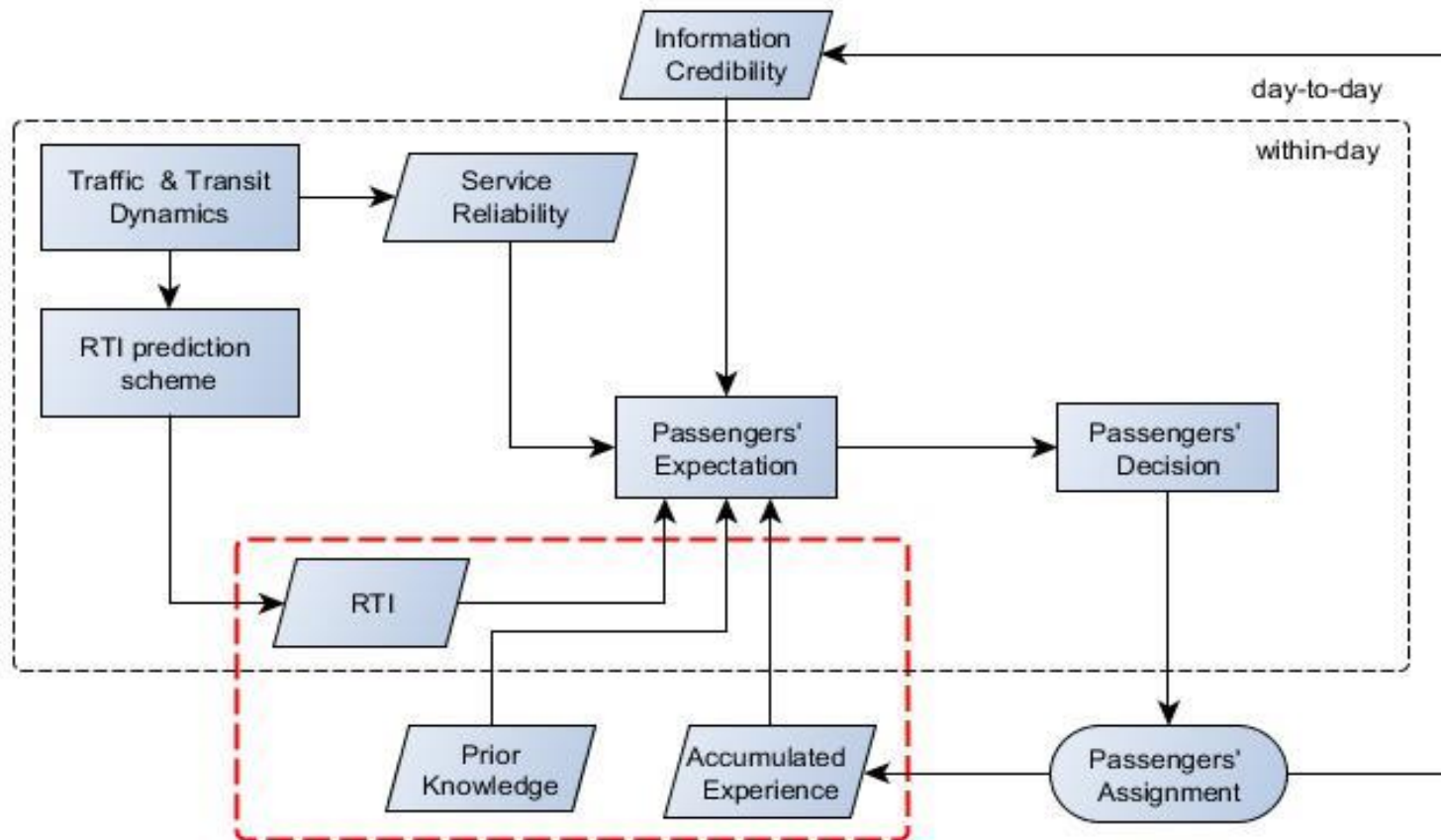
Real-time Travel Information: Predicting, disseminating, rerouting



Modelling Impacts of Information

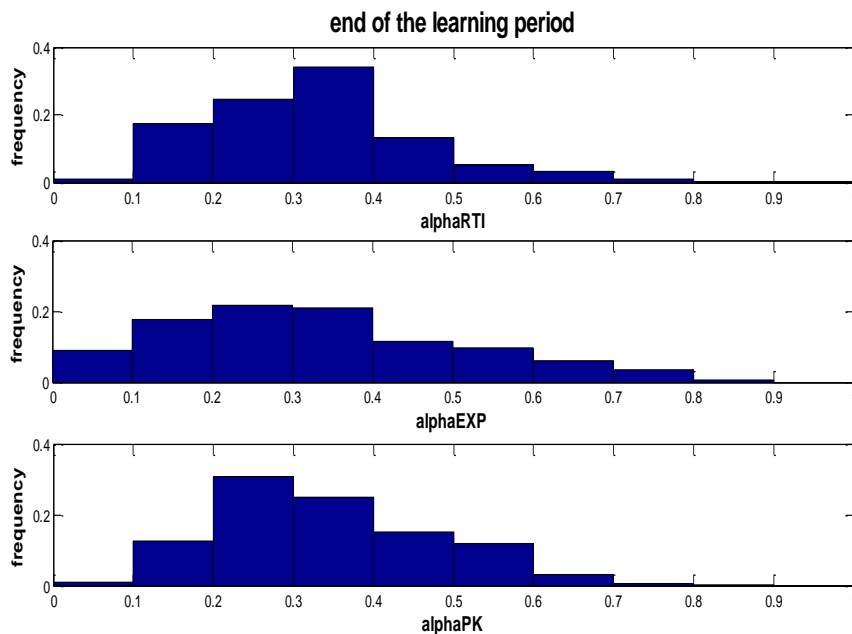


Passengers' Response to Service Reliability and Travel Information

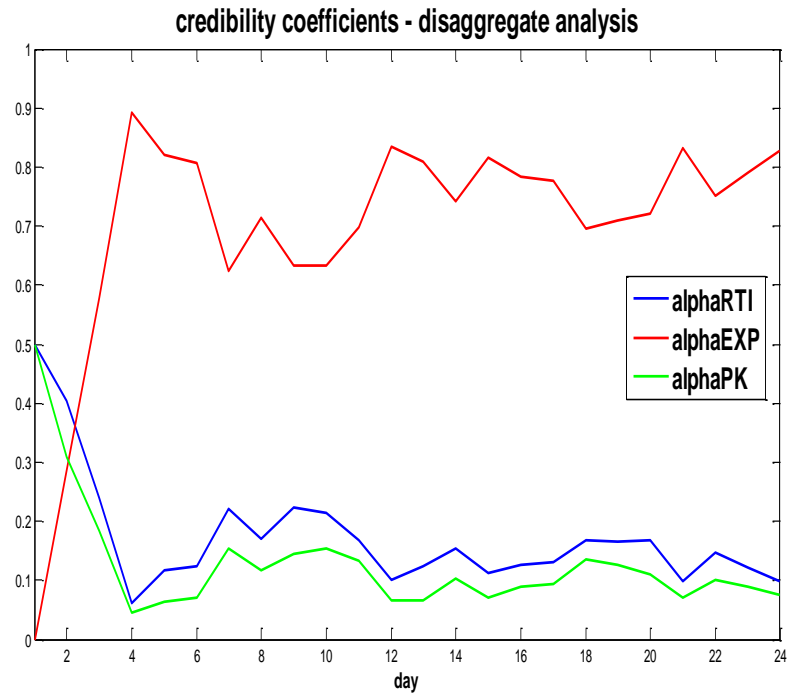


Day-to-Day Learning of Service and Information Reliability

Final distribution of credibility coeff.



Example: evolution of credibility coeff.



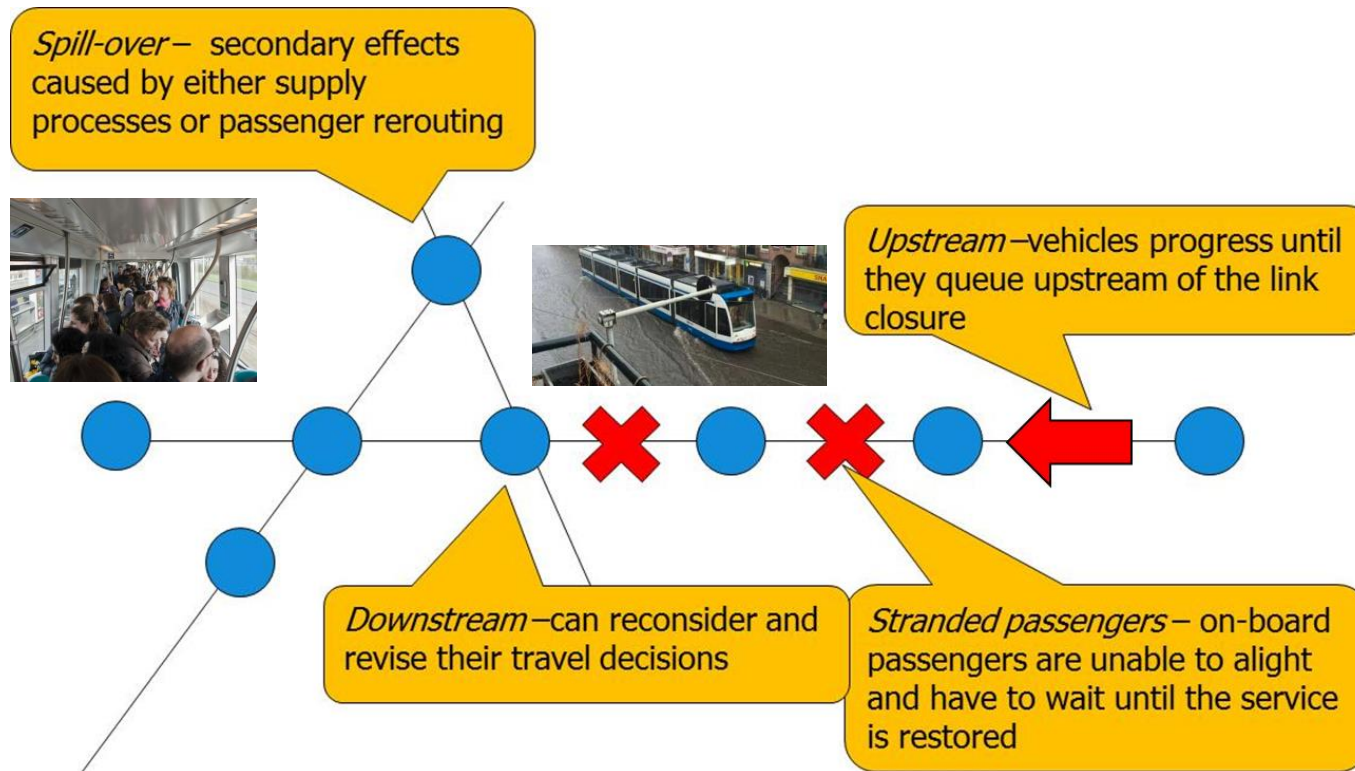
$$\alpha_{j,n}^{\lambda}(d+1) = (1 - \kappa_n^a) * \alpha_{j,n}^{\lambda}(d) + \kappa_n^a * \left(\left(\left| \frac{t_{j,n}^{e(\lambda)}(d)}{t_{j,n}^a(d)} - 1 \right| + 1 \right) \right)^{\nu}$$

*Disruptions: impact and implications
for strategic planning and operational
management*

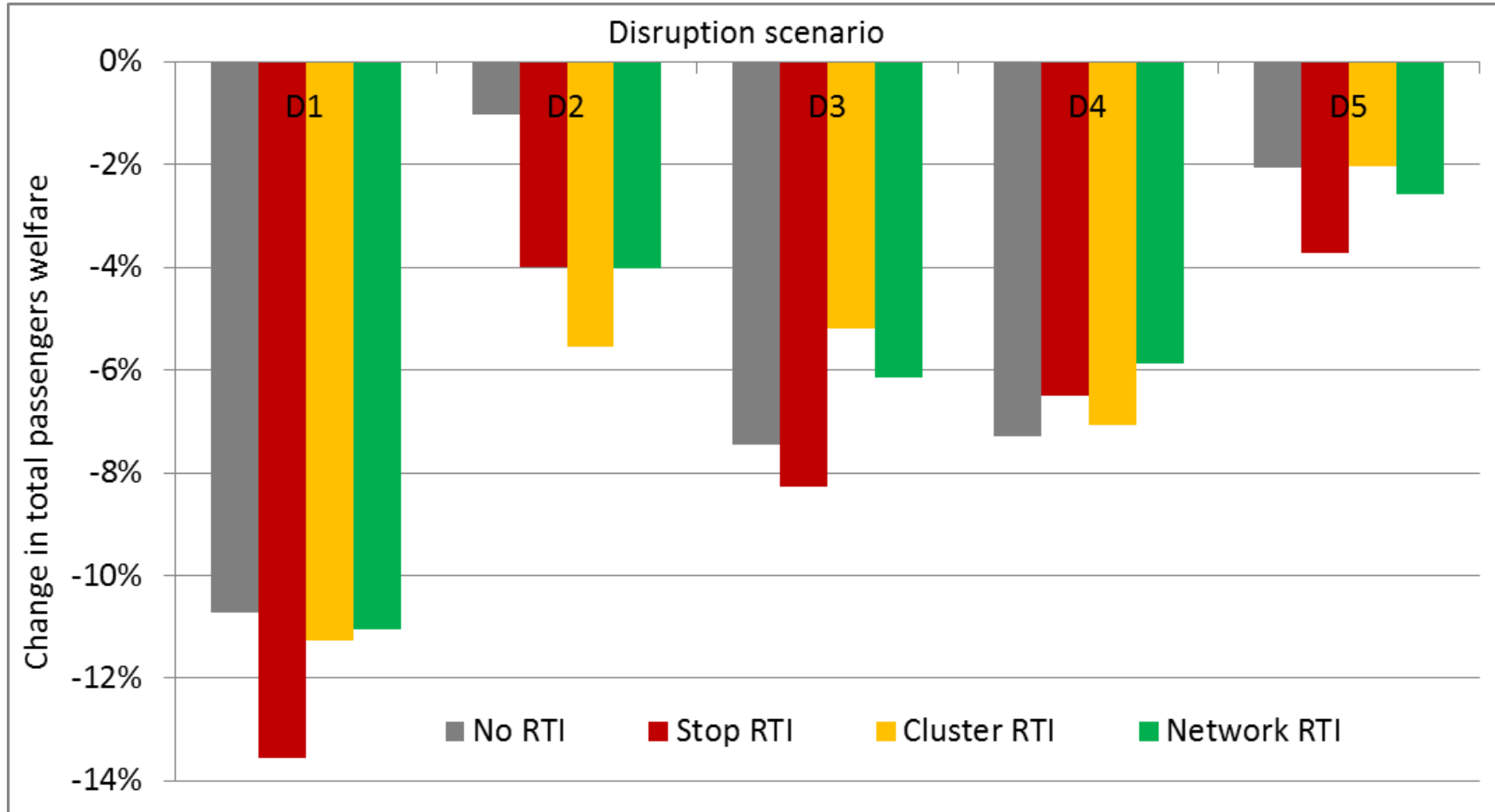


Capturing disruption dynamics

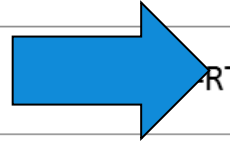
- Static model: underestimation of disruption effects
- En-route decisions, imperfect information
- Both passengers and operators can respond to disruptions



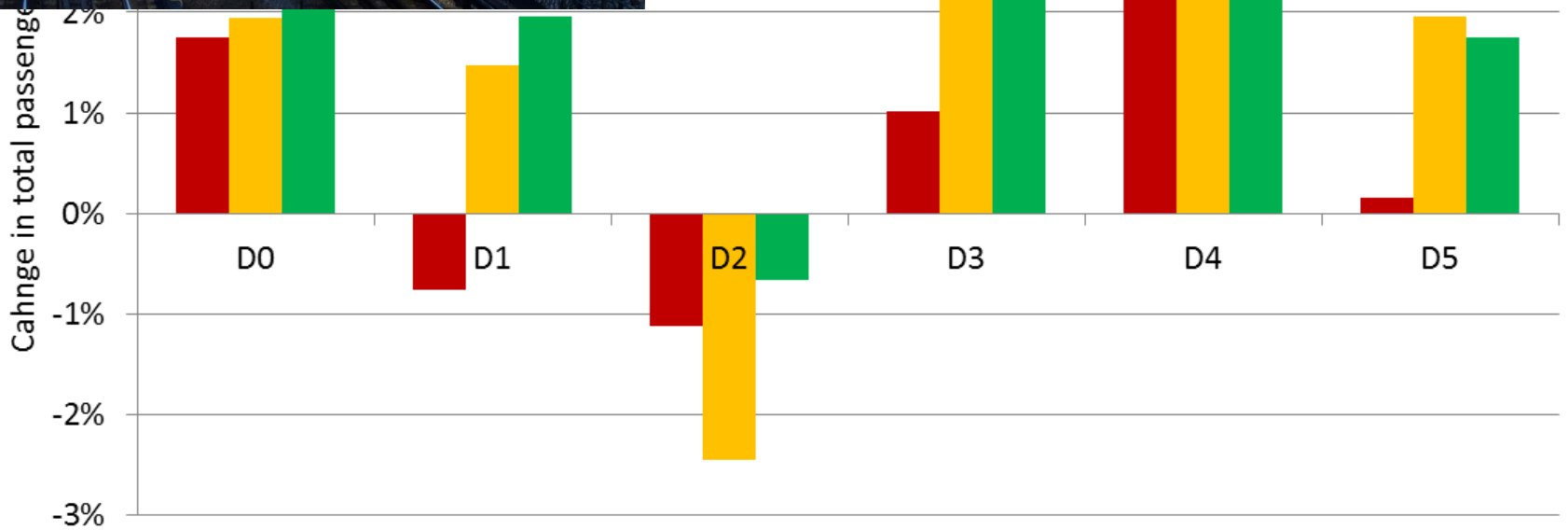
Criticality: Relative welfare loss



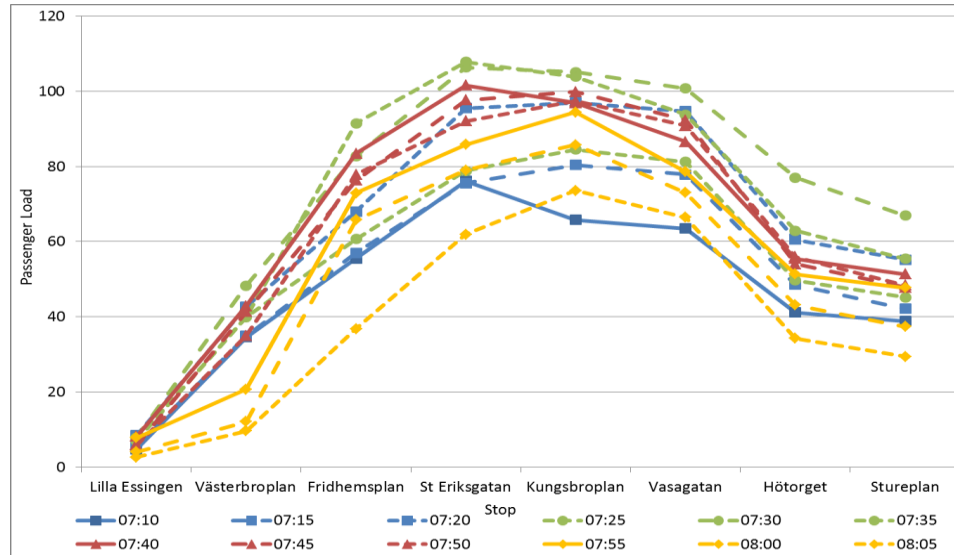
Value of Real-time information: Relative welfare gain



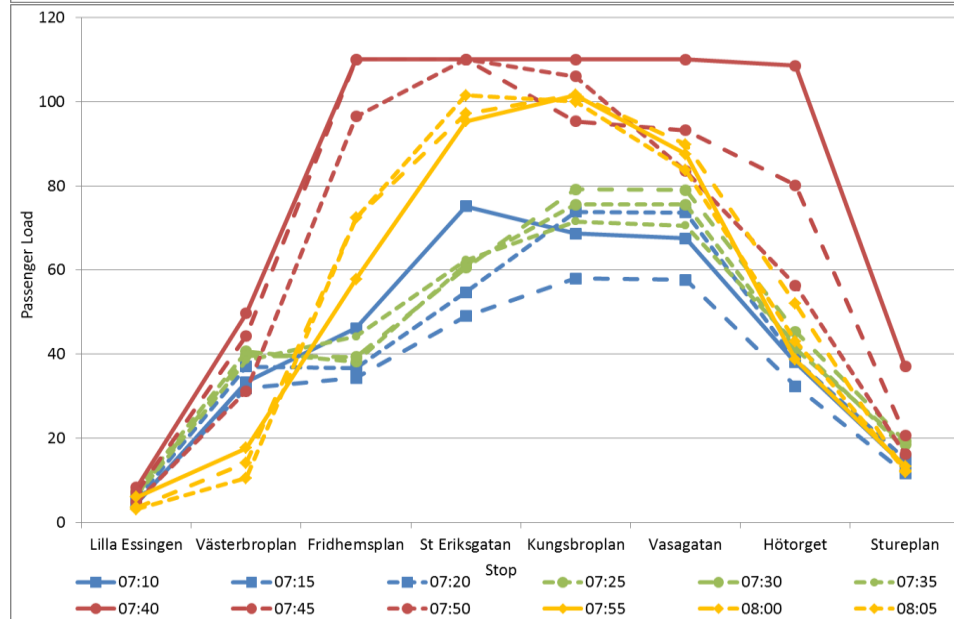
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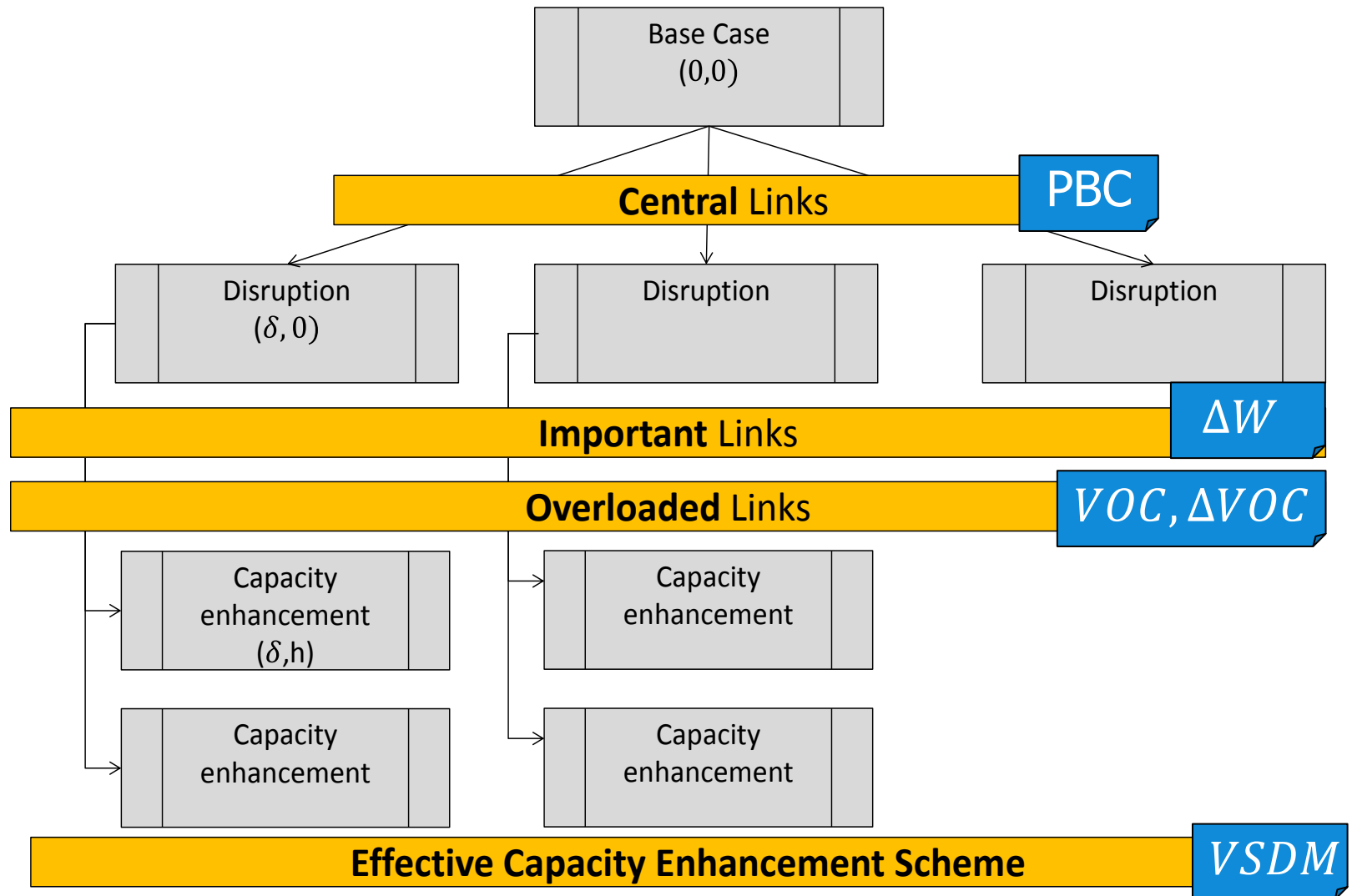
Normal operations



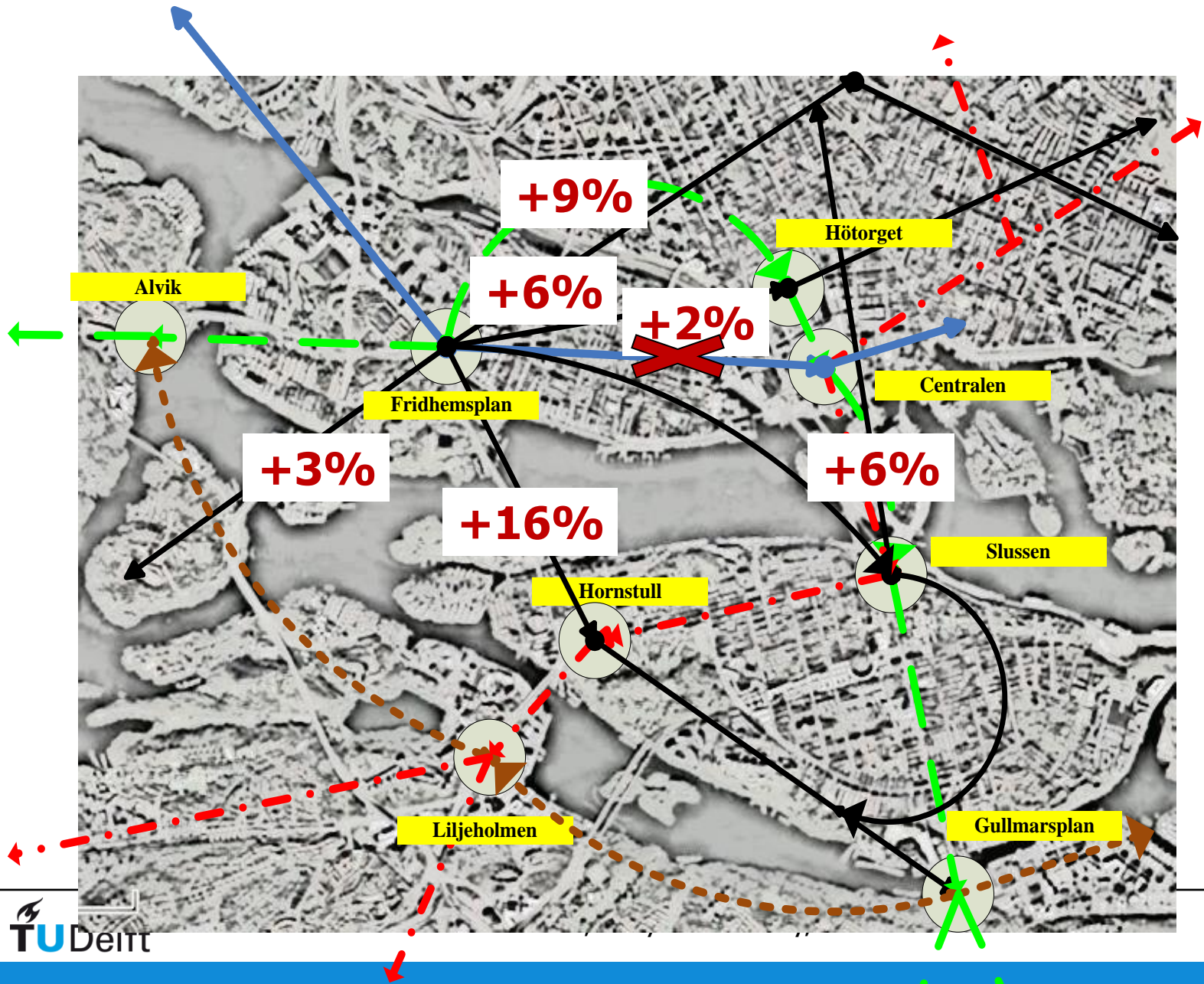
Disruption (D4)



Evaluation framework



Where shall we increase capacity?

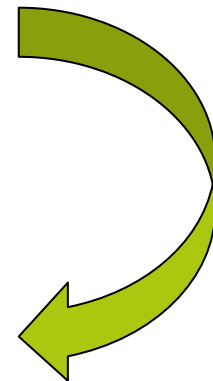


Impact indicators

	$h = 0$ Base network	$h \neq 0$ Extended network	VCE Value of capacity enhancement
$\delta = 0$ Undisrupted	$W(0,0)$	$W(0,h)$	$VCE(h 0)$ $= W(0,h)$ $- W(0,0)$
$\delta \neq 0$ Disrupted	$W(\delta,0)$	$W(\delta,h)$	$VCE(h \delta)$ $= W(\delta,h)$ $- W(\delta,0)$
PI Passenger importance	$PI(\delta 0)$ $= W(\delta,0)$ $- W(0,0)$	$PI(\delta h)$ $= W(\delta,h)$ $- W(0,h)$	
$VSDM$ Value of strategic disruption mitigation	$VSDM(h \delta) = PI(\delta h) - PI(\delta 0)$		

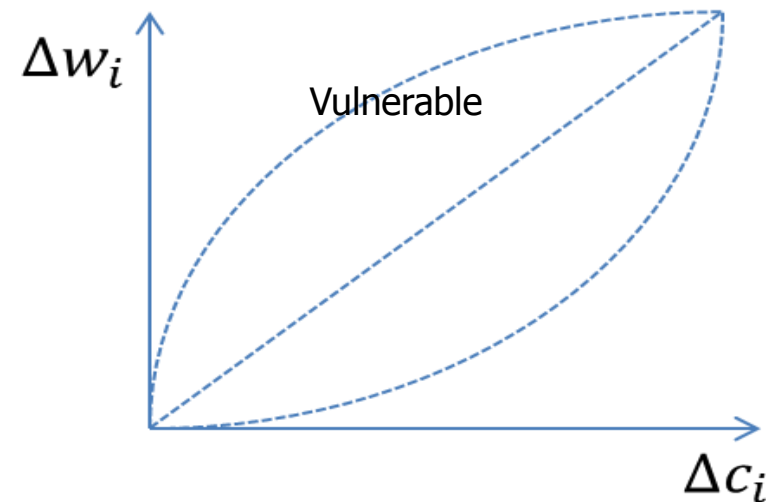
Evaluation example

R – Stop-level		Disruption (D-Blue)		Value of strategic disruption mitigation
		No	Yes	
Capacity enhancement (C-Green)	No	$w(0,0)$	$w(\delta, 0)$	+7.06%
	Yes	$w(0, h)$	$w(\delta, h)$	+2.77%
Value of capacity enhancement		-24.67%	-27.69% (planned)	

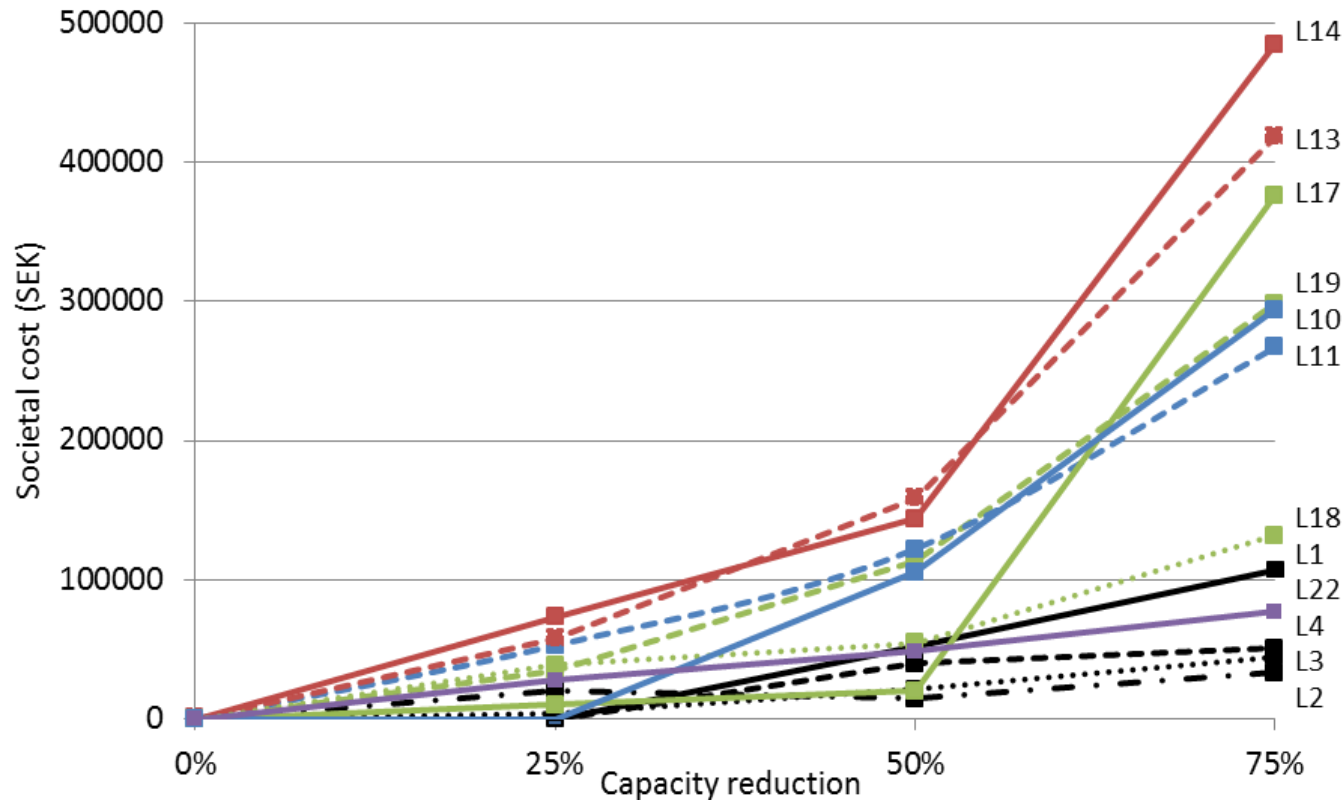


Beyond a complete failure

- Most disruptions do not amount to complete breakdowns (maintenance and construction works, traffic incidents or cancelled services)
- Vulnerable systems - greater negative impacts in a disproportional relation to the increase in the original capacity reduction
- Non-linear properties of network effects, traffic dynamics and route choice -> non-trivial relation?
- Systems that operate close to capacity
- Line-level; full-scan; dynamic assignment



Relation between capacity reduction and change in societal cost



- Long and small rather than short and large capacity reductions
- The same capacity increase counts more when relieving a larger capacity reduction

On-going research

- Modelling
 - Day to day congestion equilibrium conditions
 - Habit formation and limited adaptation
 - Passenger groups
 - Real-time dynamic control optimization

- Applications
 - Transfer coordination strategies
 - Fleet management strategies
 - Paris and Amsterdam networks

Thank you! Questions?

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