Behavior Models and Optimization

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October 14, 2017



Outline

Demand and supply

Disaggregate demand models

- 3 Literature
 - A generic framework



- Example: one theater
- Example: two theaters
- Case study
- Conclusion



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Demand models



- Supply = infrastructure
- Demand = behavior, choices
- Congestion = mismatch



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Demand models



- Usually in OR:
- optimization of the supply
- for a given (fixed) demand



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Aggregate demand



- Homogeneous population
- Identical behavior
- Price (P) and quantity (Q)
- Demand functions: P = f(Q)
- Inverse demand: $Q = f^{-1}(P)$



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Disaggregate demand



- Heterogeneous population
- Different behaviors
- Many variables:
 - Attributes: price, travel time, reliability, frequency, etc.
 - Characteristics: age, income, education, etc.
- Complex demand/inverse demand functions.



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Demand-supply interactions

Operations Research

- Given the demand...
- configure the system

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Johnson City E	nterprise.
Published Every S	aturday,
\$1. per year-Advance	Payment.
SATURDAY, APRI	L 7, 1883.
TIME TABLE	
E. T., V. & G	. R. R.
PASSENGER,	ARRIVES,
No. 1, West,	6:37, a. m.
No. 2, East,	9:45, p. m.
No. 3, West,	11:51, p.m.
No. 4, East,	o:56, a. m.
LOCAL FREIGHT,	ARRIVES,
No. 5,	1:20, a. m.
JNO. W. EAKIN	, Agent.
E. T. & W. N. C	. R. R.
Passenger, leaves,	7, a. m.
" arrives,	6, p. m.

Behavioral models

- Given the configuration of the system...
- predict the demand



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Demand-supply interactions

Multi-objective optimization



Maximize satisfaction





Outline



Disaggregate demand models

- Literature
 - A generic framework





Conclusior



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Choice models



Behavioral models

- Demand = sequence of choices
- Choosing means trade-offs
- In practice: derive trade-offs from choice models



Choice models

Theoretical foundations

- Random utility theory
- Choice set: C_n
- $y_{in} = 1$ if $i \in C_n$, 0 if not

 $P(i|\mathcal{C}_n) = \frac{y_{in} e^{v_{in}}}{\sum_{j \in \mathcal{C}} y_{jn} e^{V_{jn}}}$

• Logit model:







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Logit model

Utility

$$U_{in} = V_{in} + \varepsilon_{in}$$

Choice probability
$$P_n(i|\mathcal{C}_n) = \frac{y_{in}e^{V_{in}}}{\sum_{j\in\mathcal{C}}y_{jn}e^{V_{jn}}}.$$

- Decision-maker n
- Alternative $i \in C_n$



Variables: $x_{in} = (p_{in}, z_{in}, s_n)$

Attributes of alternative i: zin

- Cost / price (p_{in})
- Travel time
- Waiting time
- Level of comfort
- Number of transfers
- Late/early arrival
- etc.

Characteristics of decision-maker n: s_n

- Income
- Age
- Sex
- Trip purpose
- Car ownership
- Education
- Profession
- etc.



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Demand curve



Outline

Demand and supply

Disaggregate demand models

Literature

3

A generic framework

5 A simple example

- Example: one theater
- Example: two theaters

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- Case study
- Conclusior



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Stochastic traffic assignment



Features

- Nash equilibrium
- Flow problem
- Demand: path choice
- Supply: capacity



Selected literature

- [Dial, 1971]: logit
- [Daganzo and Sheffi, 1977]: probit
- [Fisk, 1980]: logit
- [Bekhor and Prashker, 2001]: cross-nested logit
- and many others...



Revenue management



Features

- Stackelberg game
- Bi-level optimization
- Demand: purchase
- Supply: price and capacity



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Selected literature

- [Labbé et al., 1998]: bi-level programming
- [Andersson, 1998]: choice-based RM
- [Talluri and Van Ryzin, 2004]: choice-based RM
- [Gilbert et al., 2014a]: logit
- [Gilbert et al., 2014b]: mixed logit
- [Azadeh et al., 2015]: global optimization
- and many others...



Facility location problem



Features

- Competitive market
- Opening a facility impact the costs
- Opening a facility impact the demand
- Decision variables: availability of the alternatives

$$P_n(i|\mathcal{C}_n) = rac{y_{in}e^{V_{in}}}{\sum_{j\in\mathcal{C}}y_{jn}e^{V_{jn}}}.$$



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Selected literature

- [Hakimi, 1990]: competitive location (heuristics)
- [Benati, 1999]: competitive location (B & B, Lagrangian relaxation, submodularity)
- [Serra and Colomé, 2001]: competitive location (heuristics)
- [Marianov et al., 2008]: competitive location (heuristic)
- [Haase and Müller, 2013]: school location (simulation-based)



Outline

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A linear formulation

Utility function

$$U_{in} = V_{in} + \varepsilon_{in} = \sum_{k} \beta_k x_{ink} + f(z_{in}) + \varepsilon_{in}.$$

Simulation

- Assume a distribution for ε_{in}
- E.g. logit: i.i.d. extreme value
- Draw R realizations ξ_{inr} , $r = 1, \dots, R$
- The choice problem becomes deterministic



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Scenarios

Draws

- Draw R realizations ξ_{inr} , $r = 1, \ldots, R$
- We obtain R scenarios

$$U_{inr} = \sum_{k} \beta_k x_{ink} + f(z_{in}) + \xi_{inr}.$$

- For each scenario r, we can identify the largest utility.
- It corresponds to the chosen alternative.



Capacities

- Demand may exceed supply
- Each alternative *i* can be chosen by maximum *c_i* individuals.
- An exogenous priority list is available.
- The numbering of individuals is consistent with their priority.



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Priority list

Application dependent

- First in, first out
- Frequent travelers
- Subscribers
- ...

In this framework

The list of customers must be sorted





References

- Technical report: [Bierlaire and Azadeh, 2016]
- TRISTAN presentation: [Pacheco et al., 2016]
- STRC proceeeding: [Pacheco et al., 2017]



Demand model



- Population of N customers (n)
- Choice set C(i)
- $C_n \subseteq C$: alternatives considered by customer n

Behavioral assumption

•
$$U_{in} = V_{in} + \varepsilon_{in}$$

•
$$V_{in} = \sum_{k} \beta_{ink} x^{e}_{ink} + q^{d}(x^{d})$$

• $P_{n}(i|\mathcal{C}_{n}) = \Pr(U_{in} \ge U_{jn}, \forall j \in \mathcal{C}_{n})$

Simulation

- Distribution ε_{in}
- R draws $\xi_{in1}, \ldots, \xi_{inR}$

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•
$$U_{inr} = V_{in} + \xi_{inr}$$

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Supply model



- Operator selling services to a market
 - Price *p*_{in} (to be decided)
 - Capacity c_i
- Benefit (revenue cost) to be maximized
- Opt-out option (*i* = 0)

Price characterization

- Continuous: lower and upper bound
- Discrete: price levels

Capacity allocation

- Exogenous priority list of customers
- Assumed given
- Capacity as decision variable

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MILP (in words)

MILP

max benefit subject to utility definition availability discounted utility choice capacity allocation price selection



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Outline

- Demand and supply
- 2 Disaggregate demand models
- 3 Literature
 - A generic framework





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A simple example



Context

- C: set of movies
- Population of N individuals
- Competition: staying home watching TV



One theater – homogenous population



Alternatives

- Staying home: $U_{cn} = 0 + \varepsilon_{cn}$
- My theater: $U_{mn} = -10.0 p_m + 3 + \varepsilon_{mn}$

Logit model ε_m i.i.d. EV(0,1)



Demand and revenues



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Optimization

Solver

GLPK v4.61 under PyMathProg

Data

- *N* = 1
- *R* = 1000

Results

- Optimum price: 0.276
- Demand: 57.4%
- Revenues: 0.159



Demand and revenues



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Example: one theater

Heterogeneous population



Two groups in the population

$$U_{mn} = -\beta_n p_m + c_n$$

Young fans: 2/3 $\beta_1 = -10$, $c_1 = 3$ Others: 1/3 $\beta_2 = -0.9$, $c_2 = 0$



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Demand and revenues



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Optimization

Data

- *N* = 3
- R = 500

Results

- Optimum price: 0.297
- Customer 1 (fan): 52.4% [theory: 50.8 %]
- Customer 2 (fan) : 49% [theory: 50.8 %]
- Customer 3 (other) : 45.8% [theory: 43.4 %]
- Demand: 1.472 (49%)
- Revenues: 0.437







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Demand and revenues



Two theaters, different types of films





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Two theaters, different types of films

Theater *m*

- Attractive for young people
- Star Wars Episode VII

Theater *k*

- Not particularly attractive for young people
- Tinker Tailor Soldier Spy

Heterogeneous demand

- Two third of the population is young (price sensitive)
- One third of the population is not (less price sensitive)

Two theaters, different types of films

Data

- Theaters *m* and *k*
- *N* = 9
- *R* = 50
- $U_{mn} = -10p_m + 4$, n = young
- $U_{mn} = -0.9p_m$, n =others
- $U_{kn} = -10p_k + (0)$, n =young
- $U_{kn} = -0.9p_k$, n =others

Theater *m*

- Optimum price m: 0.390
- Young customers: 3.48 / 6
- Other customers: 1.08 / 3
- Demand: 4.56 (50.7%)
- Revenues: 1.779

Theater k

- Optimum price k: 1.728
- Young customers: 0.0 / 6
- Other customers: 0.38 / 3

- Demand: 0.38 (4.2%)
- Revenues: 0.581

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Theater k

Cheap (half price)Star Wars Episode VIII

Two theaters, same type of films

Theater *m*

- Expensive
- Star Wars Episode VII

Heterogeneous demand

- Two third of the population is young (price sensitive)
- One third of the population is not (less price sensitive)

Two theaters, same type of films

Data

- Theaters *m* and *k*
- *N* = 9
- *R* = 50
- $U_{mn} = -10p + (4)$, n =young
- $U_{mn} = -0.9p$, n =others
- $U_{kn} = -10p/2 + (4)$, n =young
- $U_{kn} = -0.9p/2$, *n* =others

Theater *m*

- Optimum price m: 3.582
- Young customers: 0
- Other customers: 1.9
- Demand: 1.9 (31.7%)
- Revenues: 3.42

Theater *k* Closed

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Outline

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Challenge

- Select a real choice model from the literature
- Integrate it in an optimization problem.

Parking choices



- N = 50 customers
- $C = \{PSP, PUP, FSP\}$
- $C_n = C \quad \forall n$

- PSP: 0.50, 0.51, ..., 0.65 (16 price levels)
- PUP: 0.70, 0.71, ..., 0.85 (16 price levels)
- Capacity of 20 spots

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Case study

Choice model: mixtures of logit model [lbeas et al., 2014]

$$V_{FSP} = (\beta_{AT})AT_{FSP} + [\beta_{TD}]TD_{FSP} + [\beta_{Origin_{INT_FSP}}]Origin_{INT_FSP}$$

$$V_{PSP} = [ASC_{PSP}] + (\beta_{AT})AT_{PSP} + [\beta_{TD}]TD_{PSP} + (\beta_{FEE})FEE_{PSP}$$

$$+ [\beta_{FEE_{PSP(Lowlnc)}}]FEE_{PSP}LowInc + [\beta_{FEE_{PSP(Res)}}]FEE_{PSP}Res$$

$$V_{PUP} = [ASC_{PUP}] + (\beta_{AT})AT_{PUP} + [\beta_{TD}]TD_{PUP} + (\beta_{FEE})FEE_{PUP}$$

$$+ [\beta_{FEE_{PUP(Lowlnc)}}]FEE_{PUP}LowInc + [\beta_{FEE_{PUP(Res)}}]FEE_{PUP}Res$$

$$+ [\beta_{AgeVeh \leq 3}]AgeVeh_{\leq 3}$$

Parameters

- Circle: distributed parameters
- Rectangle: constant parameters
- Variables: all given but FEE (in bold)

Experiment 1: uncapacitated vs capacitated case (1)



- Capacity constraints are ignored
- Unlimited capacity is assumed

- 20 spots for PSP and PUP
- Free street parking (FSP) has unlimited capacity

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Experiment 1: uncapacitated vs capacitated case (2)

Uncapacitated



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Experiment 1: uncapacitated vs capacitated case (3)

Uncapacitated



Experiment 2: price differentiation by segmentation (1)





- Discount offered to residents
- Two scenarios (municipality)
 - Subsidy offered by the municipality
 - Operator obliged to offer reduced fees
- We expect the price to increase
 - PSP: $\{0.60, 0.64, \dots, 1.20\}$
 - PUP: {0.80, 0.84, ..., 1.40}

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Case study

Experiment 2: price differentiation by segmentation (2)

Scenario 1



Scenario 2



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Case study

Experiment 2: price differentiation by segmentation (3)

Scenario 1



Scenario 2



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Other experiments

Impact of the priority list

- Priority list = order of the individuals in the data (i.e., random arrival)
- 100 different priority lists
- Aggregate indicators remain stable across random priority lists

Benefit maximization through capacity allocation

- 4 different capacity levels for both PSP and PUP: 5, 10, 15 and 20
- Optimal solution: PSP with 20 spots and PUP is not offered
- Both services have to be offered: PSP with 15 and PUP with 5



Outline

- - A generic framework



- Example: one theater
- Example: two theaters







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Summary

Demand and supply

- Supply: prices and capacity
- Demand: choice of customers
- Interaction between the two

Discrete choice models

- Rich family of behavioral models
- Strong theoretical foundations
- Great deal of concrete applications
- Capture the heterogeneity of behavior
- Probabilistic models

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Optimization

Discrete choice models

- Non linear and non convex
- Idea: use utility instead of probability
- Rely on simulation to capture stochasticity

Proposed formulation

- Linear in the decision variables
- Large scale
- Fairly general



Ongoing research

- Decomposition methods
- Scenarios are (almost) independent from each other (except objective function)
- Individuals are also loosely coupled (except for capacity constraints)



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