

Machine Learning for Behavior Model

How to collaborate DCM and ML ?

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To develop **more better** infrastructure and services, we are conducting analysis based on behavior models.

- ❑ **Prediction Accuracy:** issue of model parameter estimation
- ❑ **Model Interpretability:** issue of understanding model (behavior)

Discrete choice model

$$P(i) = \frac{\exp(\mu V_i)}{\sum_{j \in C} \exp(\mu V_j)}$$

Source: Small data

Function: Linear

Accuracy(Model fitting): Mid (Low?)

Interpretability : High

Good understanding travel behavior ?

Machine Learning

A black rectangular box with the text "Black Box" written in white, centered within the box.

Black Box

Source: Big data

Function: Non-Linear

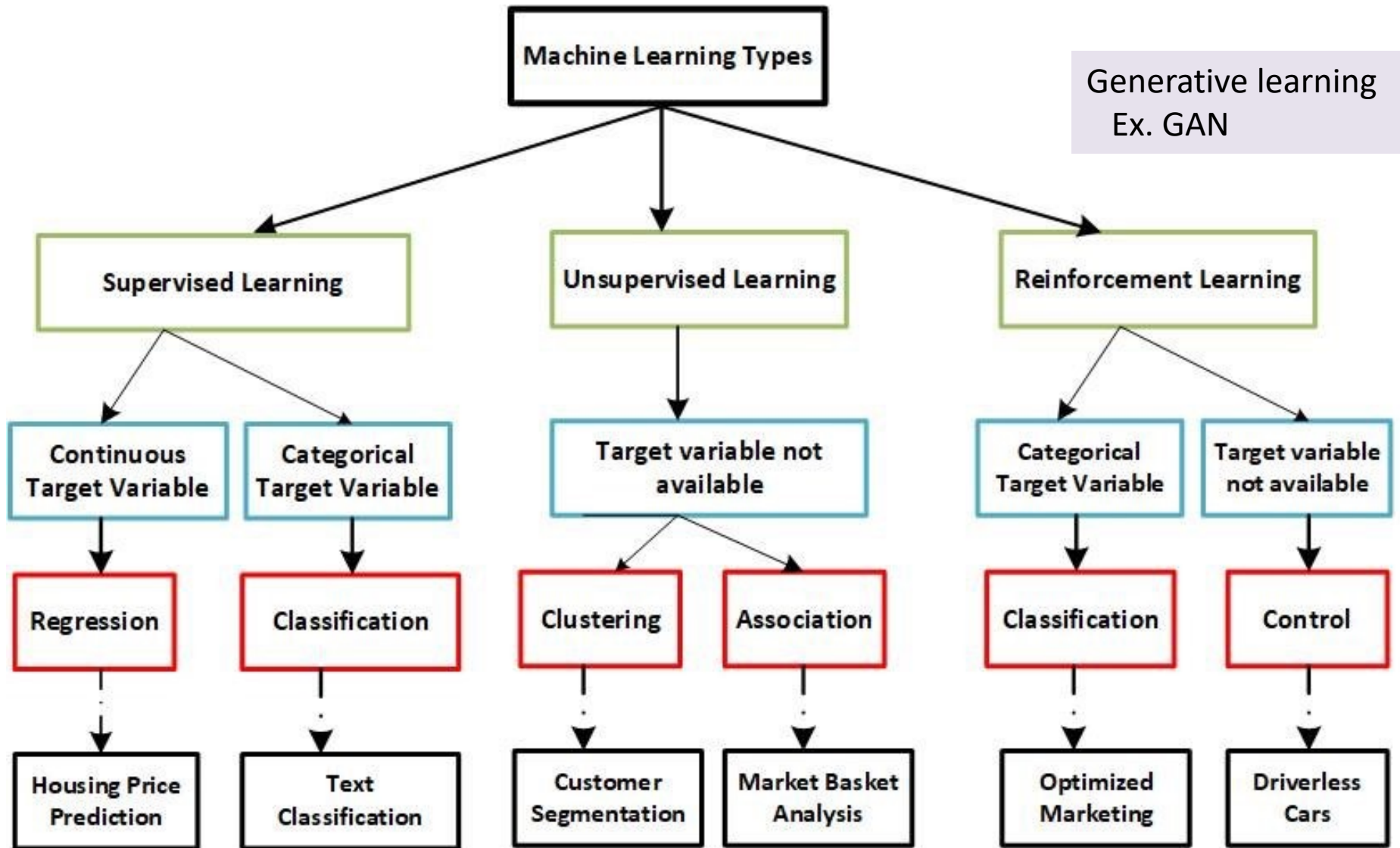
Accuracy(Model fitting): High

Interpretability: Low

NOT understanding travel behavior ?

Considering the possibility of collaboration between DCM and ML from the perspective of Accuracy and Interpretability

Overview of ML



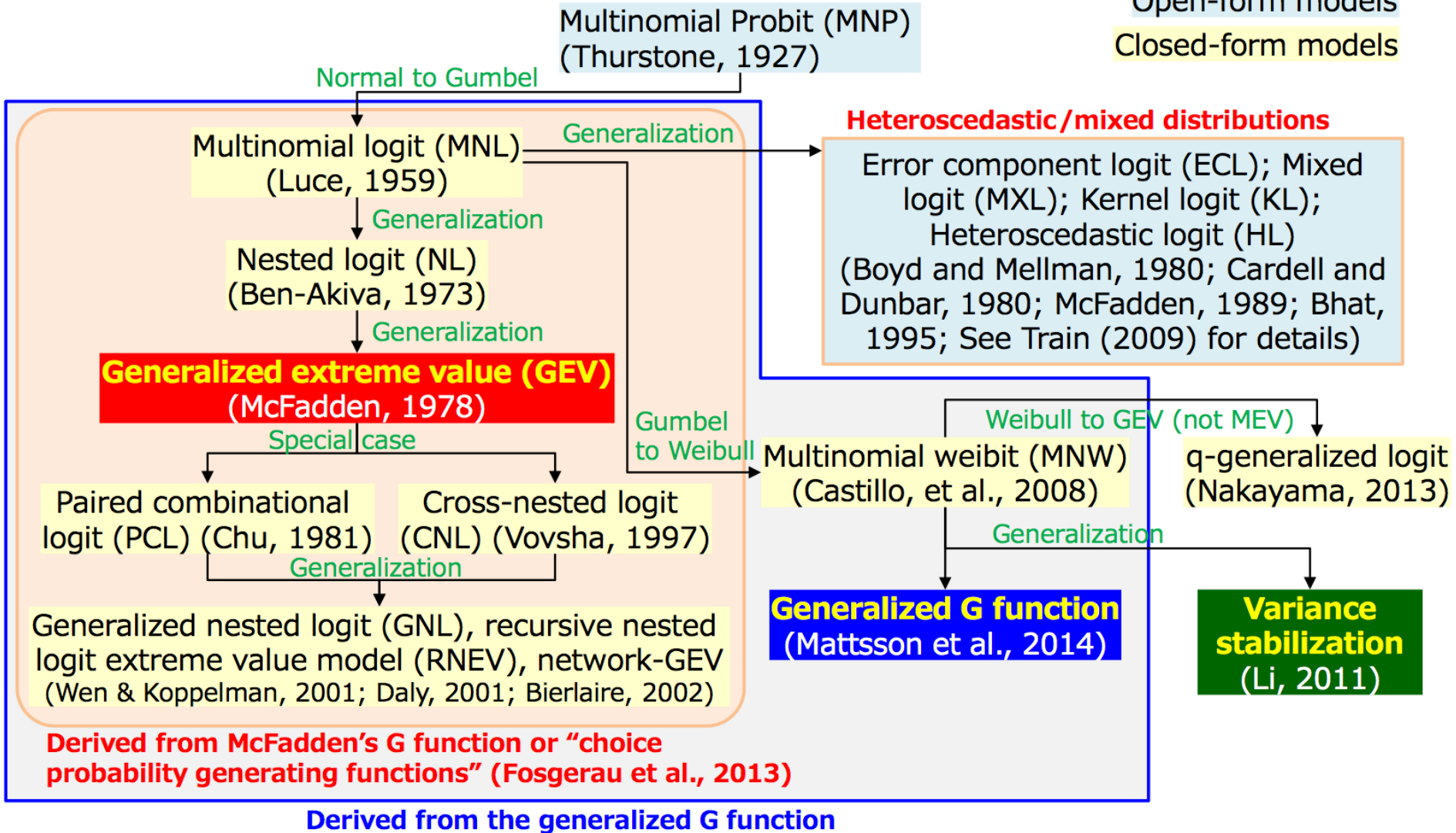
How to collaborate DCM and ML ?

Part 1: Prediction Accuracy

- You can (not) **estimate** behavior model-

Overview of DCM

Open-form models
Closed-form models



Mixed Logit (Train 2000)

High flexible model structure by **two error** term.

Utility function

$$U_i = V_i + \eta_i + v_i$$

v dist.: assume any G function

- IID Gamble (Logit Kernel) \Rightarrow MNL
- any G function (GEV Kernel) \Rightarrow NL, PCL, CNL, GNL...

η dist.: basically assume “*Normal dist.*”

In the case of normal distribution takes a non-realistic value, it can assume a variety of probability distribution (triangular distribution, cutting normal distribution, lognormal distribution, Rayleigh distribution, etc.).

- 
- Error Component: approximate to any GEV model
 - Random Coefficient: Consider the heterogeneity

Approximation of Nested Logit (NL)

Describe the nest (covariance) using structured η .

Ex: model choice

Normal \Rightarrow nest

Car : $U_{car} = \beta \mathbf{X}_{car} + v_{car}$

Bus : $U_{bus} = \beta \mathbf{X}_{bus} + \sigma_{transit} \eta_{transit} + v_{bus}$

Rail : $U_{rail} = \beta \mathbf{X}_{rail} + \sigma_{transit} \eta_{transit} + v_{rail}$

Transit nest

IID Gamble \Rightarrow Logit

Choice prob.
(open-form)

$$P_{rail} = \int_{\eta_{transit}} \frac{e^{V_{rail} + \sigma_{transit} \eta_{transit}}}{e^{V_{car}} + e^{V_{bus} + \sigma_{transit} \eta_{transit}} + e^{V_{rail} + \sigma_{transit} \eta_{transit}}} f(\eta_{transit}) d\eta_{transit}$$



Choice prob.
(Simulated)

$$P_{rail} = \frac{1}{N} \sum_N \frac{e^{V_{rail} + \sigma_{transit} \eta_{transit}^N}}{e^{V_{car}} + e^{V_{bus} + \sigma_{transit} \eta_{transit}^N} + e^{V_{rail} + \sigma_{transit} \eta_{transit}^N}}$$

$$\eta_{transit} \approx N(0,1)$$

Approximation of unobservable heterogeneity

Assume the heterogeneity of parameter

⇒ In the case of parameter following Normal dist., we estimate the dist.'s hyper-parameter (mean and variance).

$$U_{car,n} = \beta_n T_{car,n} + v_{car,n}$$

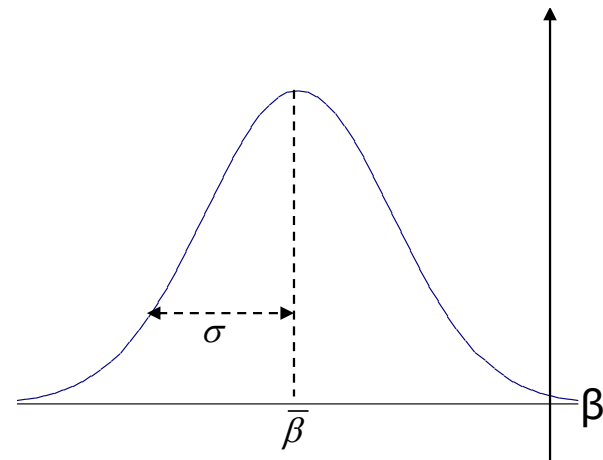
$$\beta_n \approx N(\bar{\beta}, \sigma^2)$$

$$U_{car,n} = \bar{\beta} T_{car,n} + \sigma \eta_n T_{car,n}$$

$$U_{bus,n} = \bar{\beta} T_{bus,n} + \sigma \eta_n T_{bus,n}$$

$$U_{rail,n} = \bar{\beta} T_{rail,n} + \sigma \eta_n T_{rail,n}$$

$$\eta_n \approx N(0,1) \quad \bar{\beta}, \sigma : \text{unknown parameter}$$



Hyper-parameter can describe using observable variables

$$\bar{\beta}_n = \gamma_0 + \gamma_1 \text{income}_n \quad \beta \text{ depend on observable income variable}$$

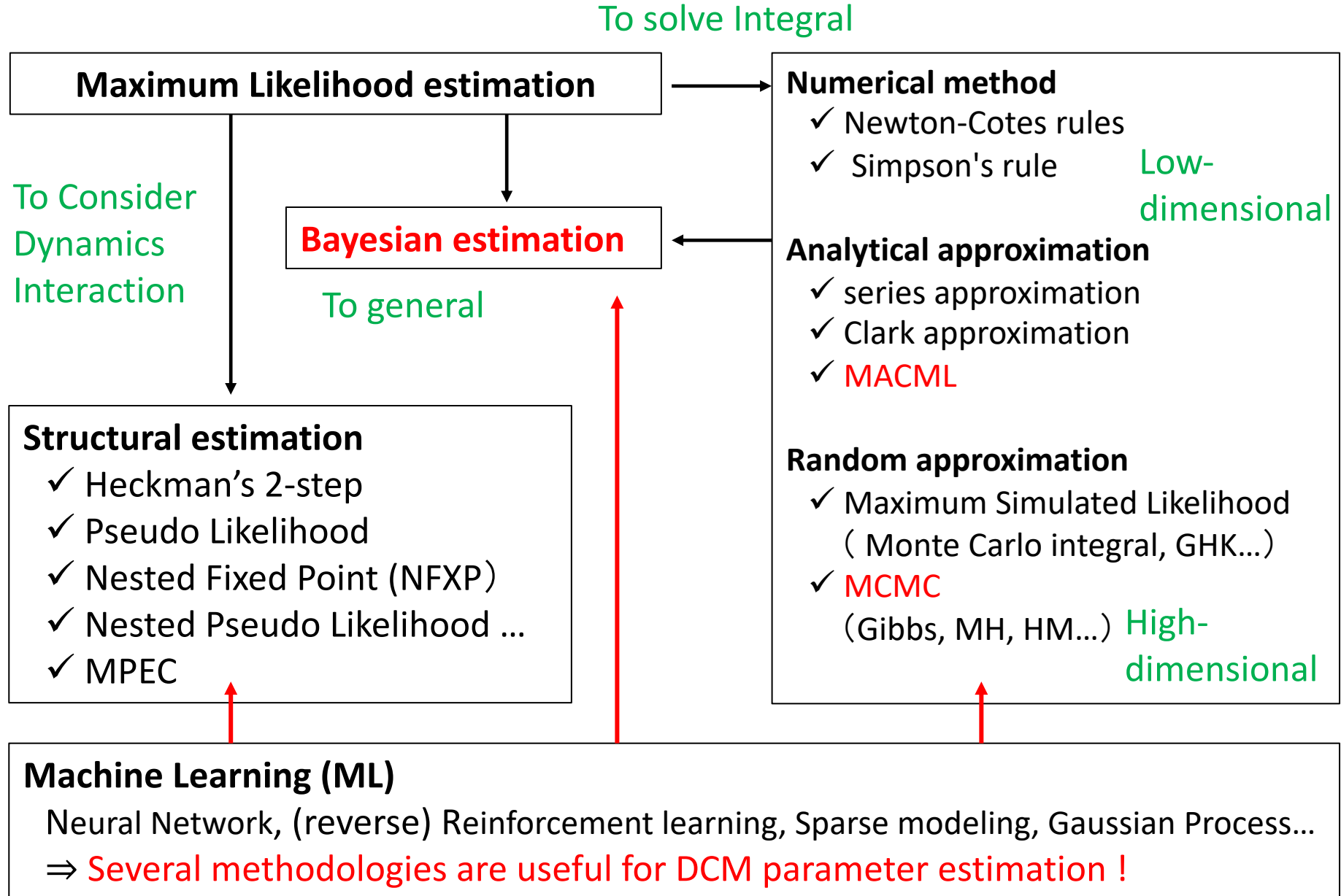
Why estimation methods is important ?

- ✓ Advance GEV model (CNL, GNL, n-GEV...) has many parameter.
⇒ Convergence becomes unstable (Hessian passed away...)
- ✓ non-GEV model requires multiple integral calculations .
⇒ ML estimation can not be used
- ✓ Stricture of utility function (non-liner, complex distribution)
- ✓ Dynamic choice behavior (Dynamic Programing: DP)
- ✓ Interaction between decision-maker (Endogeneity)
- ✓ high dimensional data ⇒ N of Sample < N of Variable

The analyst needs to select an appropriate estimation method corresponding to the model !

Overview of Estimation method

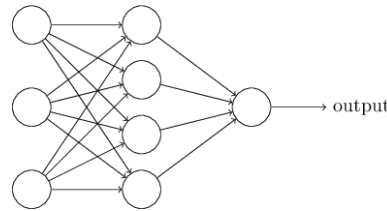
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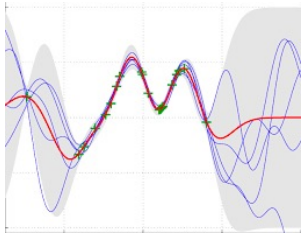
Collaboration of DCM and ML

Estimation methods in the field of machine learning can be applied to DCM estimation.

**Neural network
(Back propagation)**

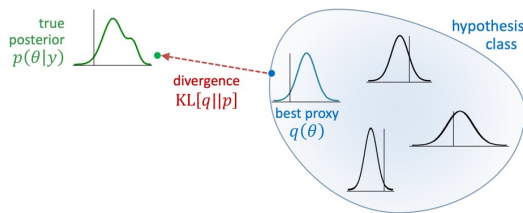


Gaussian Process



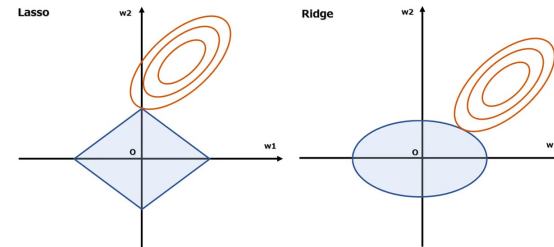
Estimation considering complex nonlinear structures

Variational Bayesian



Estimation considering complex probability distribution

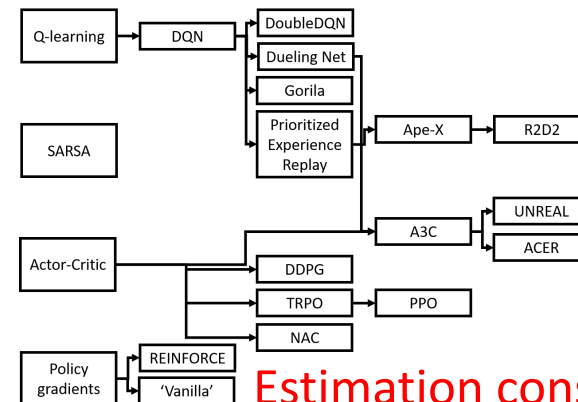
Sparse modeling



Estimation considering parameter dimension reduction



Reinforcement learning



Estimation considering complex and dynamic choice

How to collaborate DCM and ML ?

Part 2: Model Interpretability

- You can (not) **understand** behavior model-

Recent issue in AI

- ◆ In recent years, accuracy and explainability of AI (ML) has been required in practice situation.
 - ◆ XAI: provides **reasons and evidence** that humans can understand for the results by AI.
 - ◆ Three requirements were presented in G20 AI principles
- Human centered values
- Fairness (公平性)
 - Accountability (説明責任)
 - Transparency (透明性)

https://www.mofa.go.jp/policy/economy/g20_summit/osaka19/en/documents/final_g20_osaka_leaders_declaration.html

ANNEX

G20 AI Principles ¹

The G20 supports the Principles for responsible stewardship of Trustworthy AI in Section 1 and takes note of the Recommendations in Section 2.

Section 1: Principles for responsible stewardship of trustworthy AI

1.1. Inclusive growth, sustainable development and well-being

Stakeholders should proactively engage in responsible stewardship of trustworthy AI in pursuit of beneficial outcomes for people and the planet, such as augmenting human capabilities and enhancing creativity, advancing inclusion of underrepresented populations, reducing economic, social, gender and other inequalities, and protecting natural environments, thus invigorating inclusive growth, sustainable development and well-being.

1.2. Human-centered values and fairness

- a) AI actors should respect the rule of law, human rights and democratic values, throughout the AI system lifecycle. These include freedom, dignity and autonomy, privacy and data protection, non-discrimination and equality, diversity, fairness, social justice, and internationally recognized labor rights.
- b) To this end, AI actors should implement mechanisms and safeguards, such as capacity for human determination, that are appropriate to the context and consistent with the state of art.

1.3. Transparency and explainability

AI Actors should commit to transparency and responsible disclosure regarding AI systems. To this end, they should provide meaningful information, appropriate to the context, and consistent with the state of art:

- i. to foster a general understanding of AI systems;
- ii. to make stakeholders aware of their interactions with AI systems, including in the workplace;
- iii. to enable those affected by an AI system to understand the outcome; and,
- iv. to enable those adversely affected by an AI system to challenge its outcome based on plain and easy-to-understand information on the factors, and the logic that served as the basis for the

Fairness

Eliminate **biases** that cause unfairness so that AI can provide fair services regardless of **differences in user attributes**.

- Bias in training data (input): historical bias, sampling bias
- Users with certain attributes cannot receive the service. And they cannot receive the same level of service as other users.

Accountability

Clarify where the **cause of the error lies** and who (or what) is responsible for it.

- In complex models, it may be difficult to identify where the cause of the problem lies. (ex. DNN)

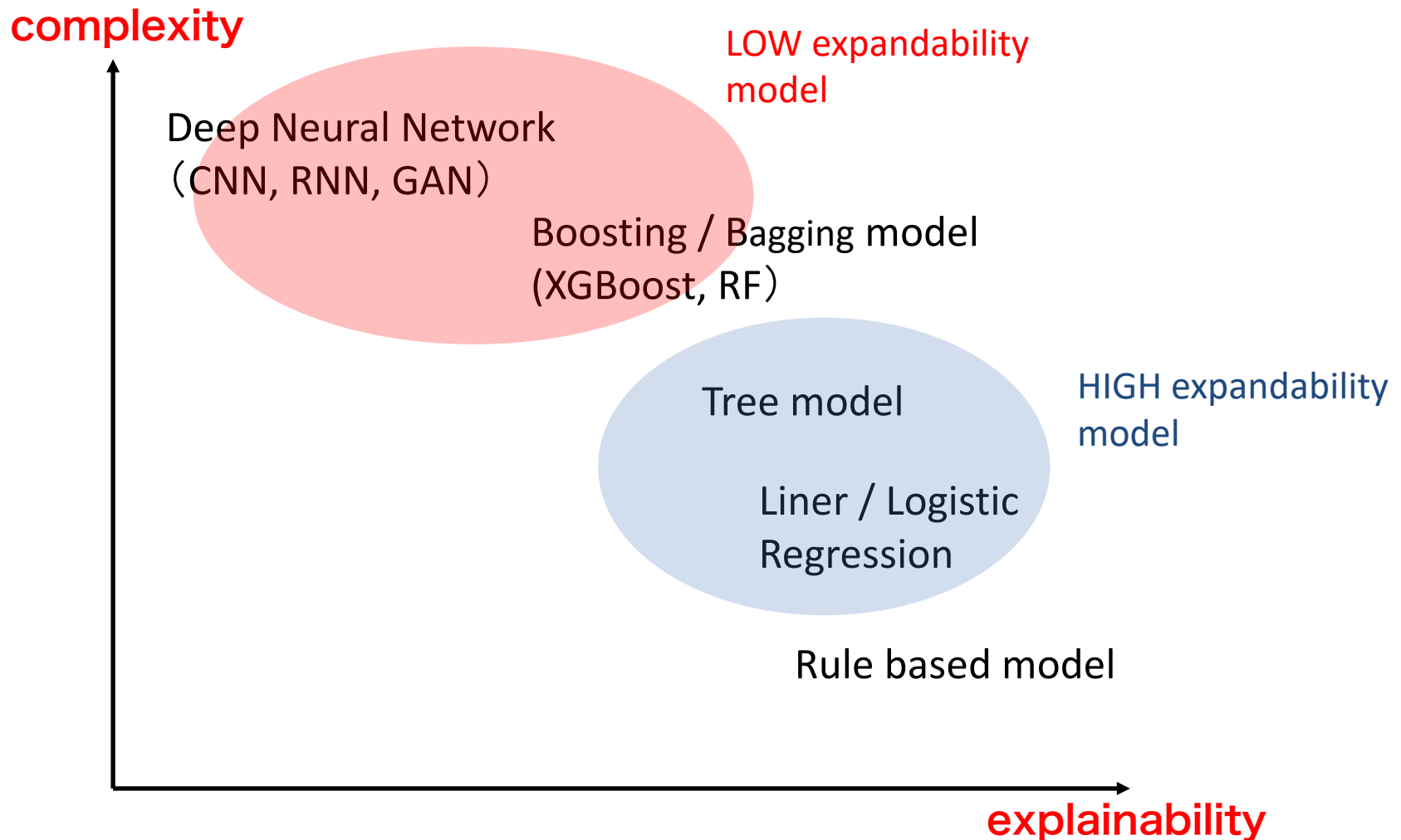
Transparency

AI systems can present information that **users can understand**.

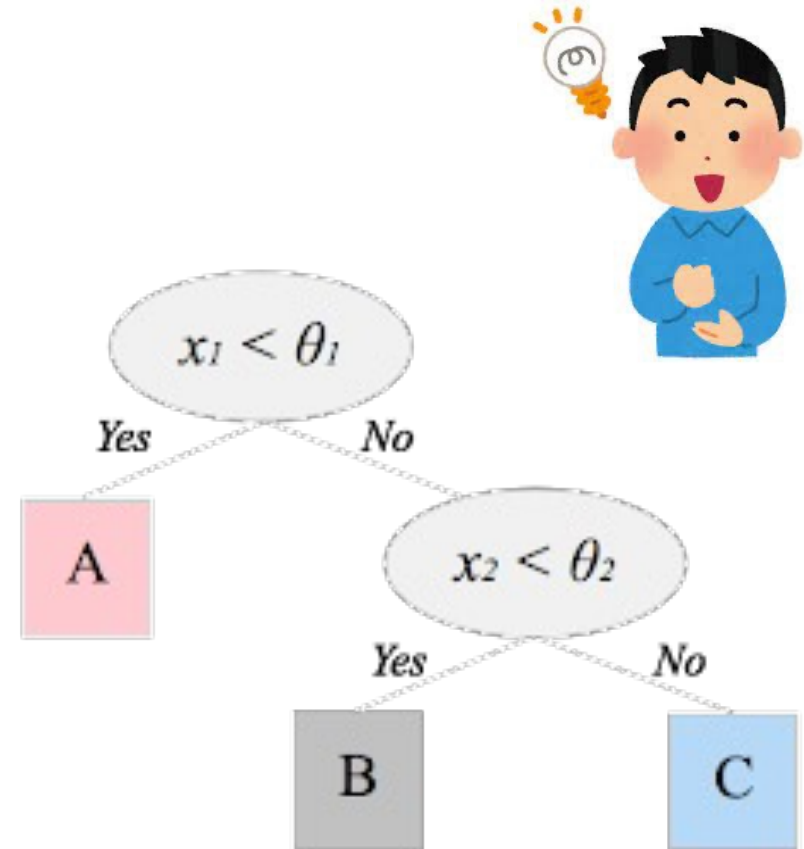
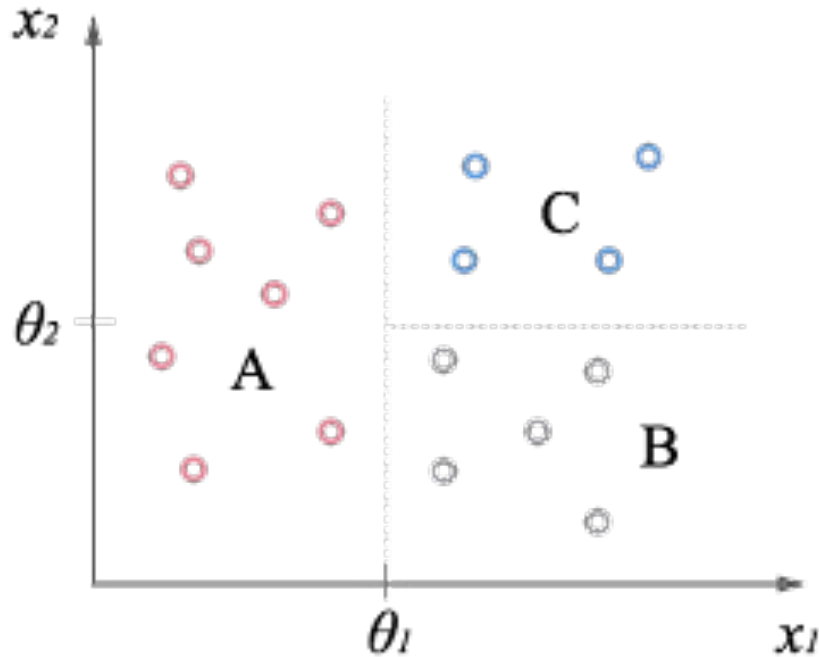
- Information that should be presented model (**processing criteria**), data was used to train it, validation, etc...
- This is important when dealing with issues related to medical, safety and policy making.

Explainability of ML methods

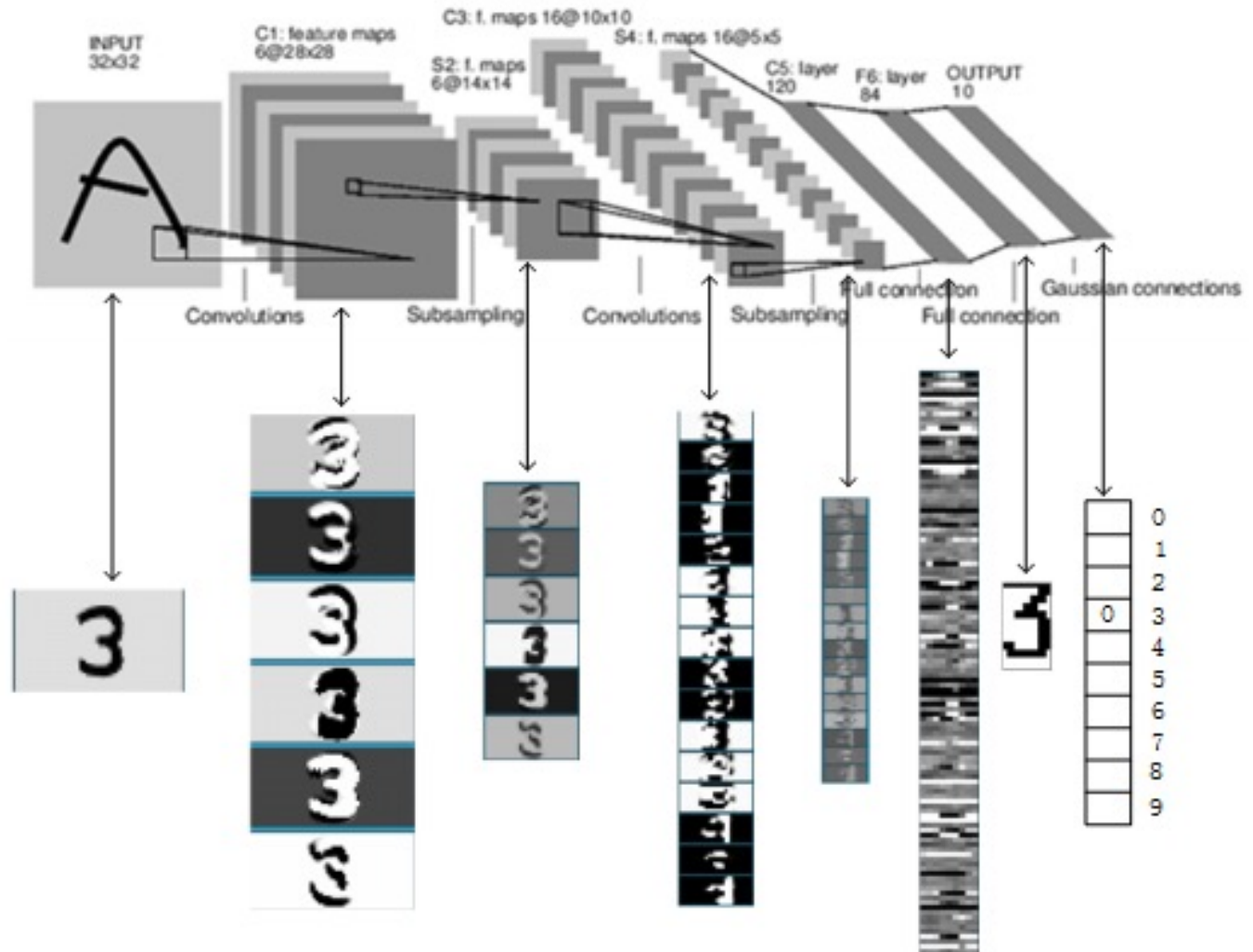
In machine learning, there is a **tradeoff** between the **complexity** (= accuracy) of the problem and its **explainability**.



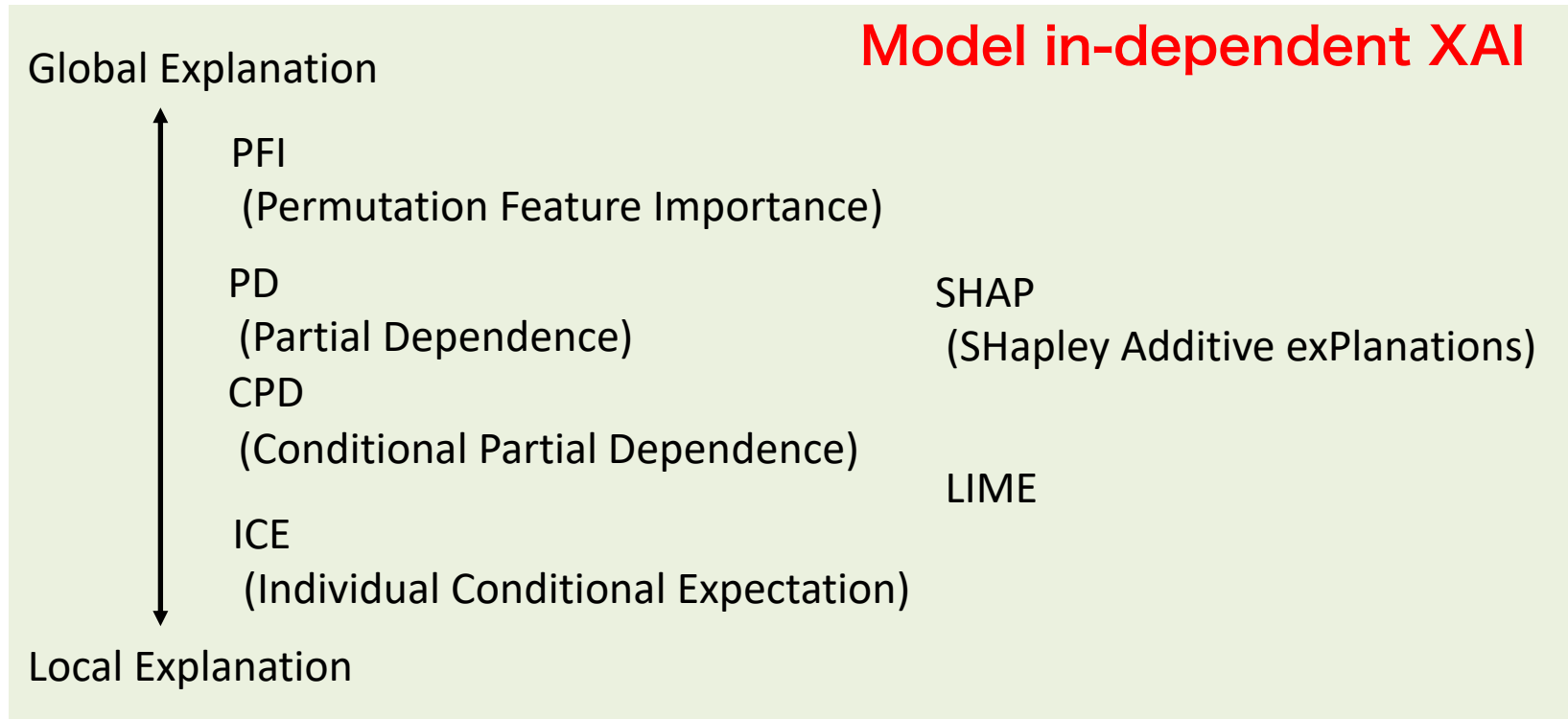
Tree model



CNN model



- ◆ Global or Local explanation: Domains that the model can explain
 - Global: Understand the overall behavior of AI models.
 - Local: Understand the reasoning behind each prediction.



Model dependent XAI

CAM/ Grad-CAM

Integrated Gradients

Tree Surrogate

Attention

PFI: Permutation Feature Importance

- ◆ Calculating the **feature importance** in models.
- ◆ Shuffle (**permutation**) the features sample data and evaluate the importance based on the **prediction error** of the model.

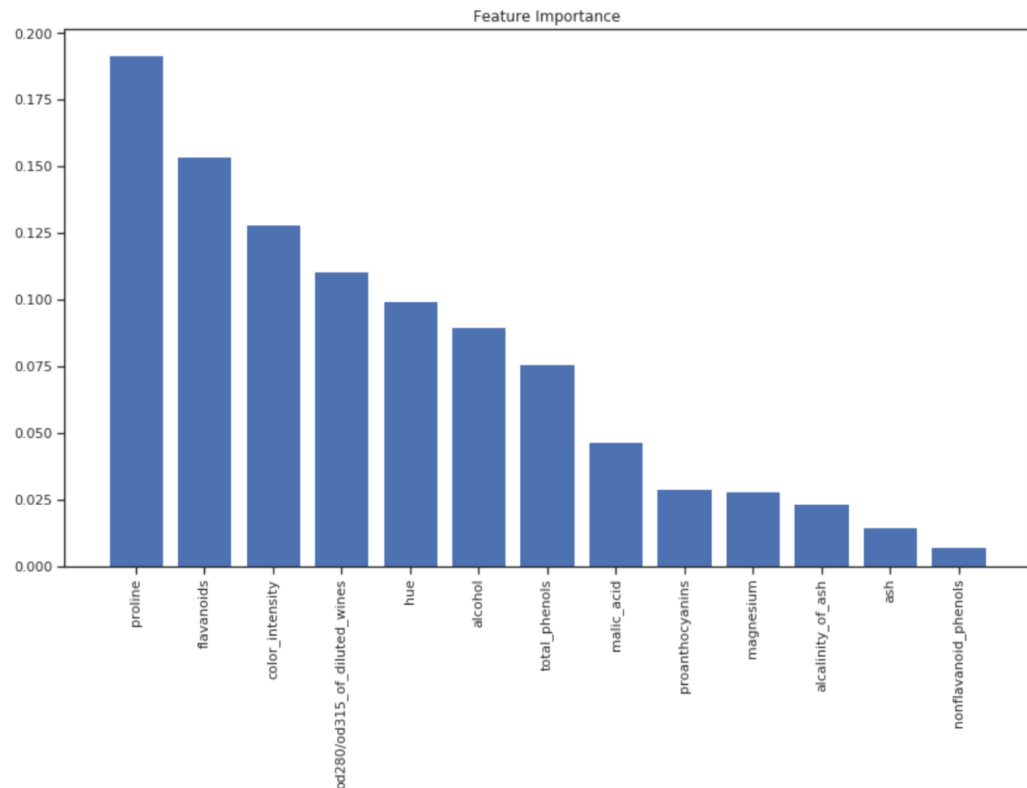
Trained model

$$y = f(x)$$

Error Function

Test data

	value_1	value_2	value_3	value_4	value_5	value_6	value_7	value_8	value_9	value_10
dataname										
data_1	12	91	30	22	39	63	75	53	17	91
data_2	29	61	87	9	24	55	57	3	11	45
data_3	59	33	28	61	86	81	52	90	29	48
data_4	11	79	16	41	30	79	57	57	25	89
data_5	75	9	84	31	50	58	21	71	74	38
...
data_121	16	94	29	60	14	95	74	14	46	2
data_122	30	70	82	58	36	44	47	90	7	85
data_123	27	29	24	9	29	4	47	94	88	43
data_124	21	66	45	33	69	99	43	91	34	78
data_125	95	39	19	89	70	38	72	29	72	52



PFI: Algorithm

◆ Calculating the **feature importance** in models.

1. Calculate Baseline Prediction Error

Baseline prediction error

$$e_{base}(f) = \mathbb{E}[L(f(x), y)]$$

Error evaluation index
(ex. RMSE)

Trained model $y = f(x)$

Obs. Value Prediction Value

2. Create feature's shuffle data

	value_1	value_2	value_3	value_4	value_5	value_6	value_7	value_8	value_9	value_10
dataname										
data_1	12	91	30	22	39	63	75	53	17	91
data_2	29	61	87	9	24	55	57	3	11	45
data_3	59	33	28	61	86	81	52	90	29	48
data_4	11	79	16	41	30	79	57	57	25	89
data_5	75	9	84	31	50	58	21	71	74	38
...
data_121	16	94	29	60	14	95	74	14	46	2
data_122	30	70	82	58	36	44	47	90	7	85
data_123	27	29	24	9	29	4	47	94	88	43
data_124	21	66	45	33	69	99	43	91	34	78
data_125	95	39	19	89	70	38	72	29	72	52

Random Shuffle

3. Calculate shuffle data's Prediction Error

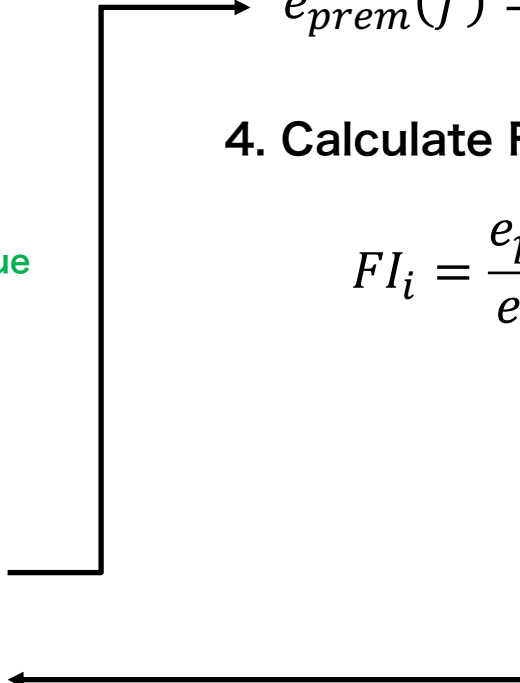
$$e_{prem}(f) = \mathbb{E}[L(f(X_i), y)]$$

4. Calculate FI index

$$FI_i = \frac{e_{prem}(f)}{e_{base}(f)}$$

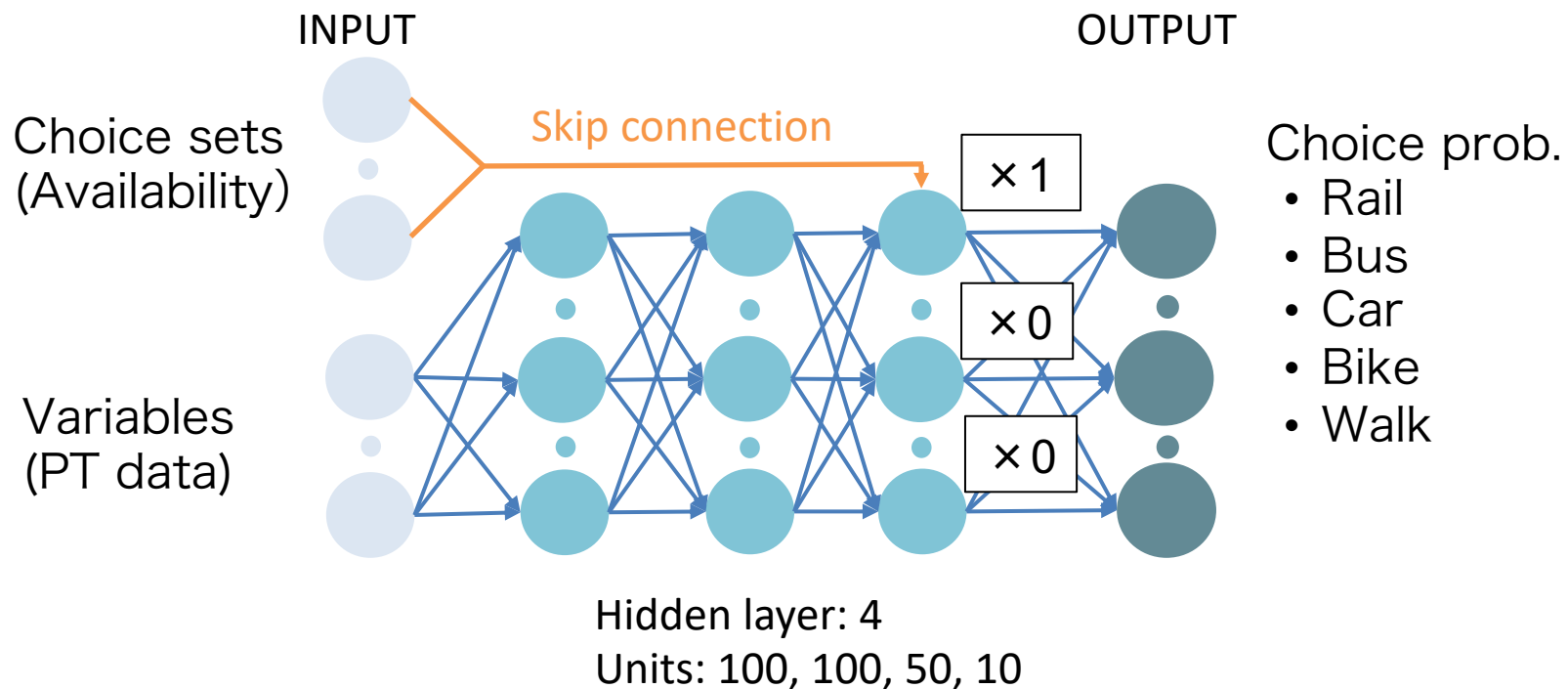
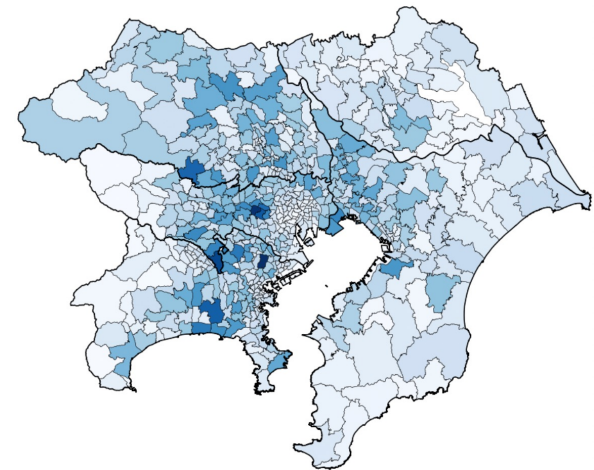
X_i

Repeat to 2-4
for all features



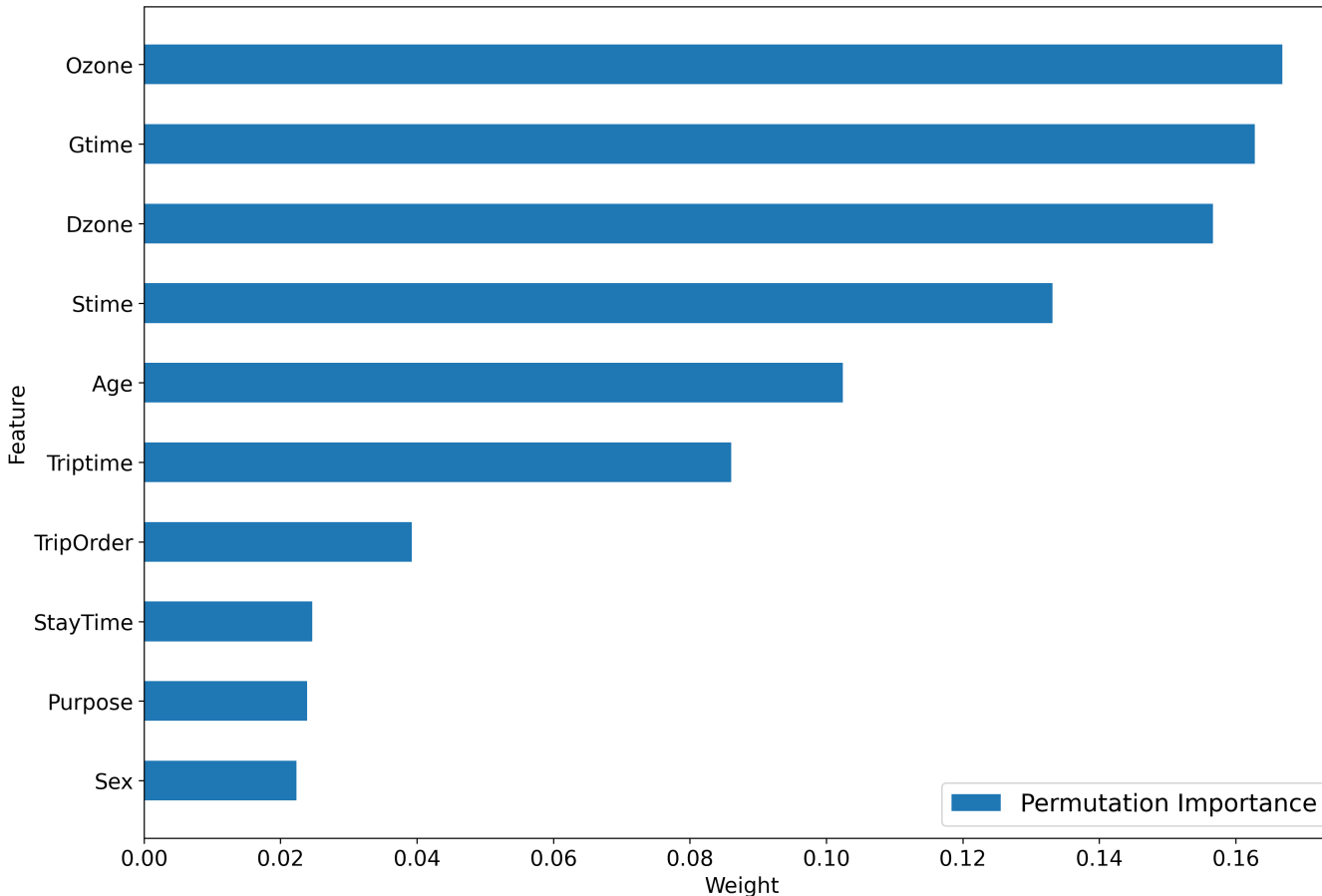
Mode choice model based on NN

- ◆ Simple NN considering choice sets by skip connection.
- ◆ Apply to the Tokyo Metropolitan area.
- ◆ Data: Tokyo PT 2018



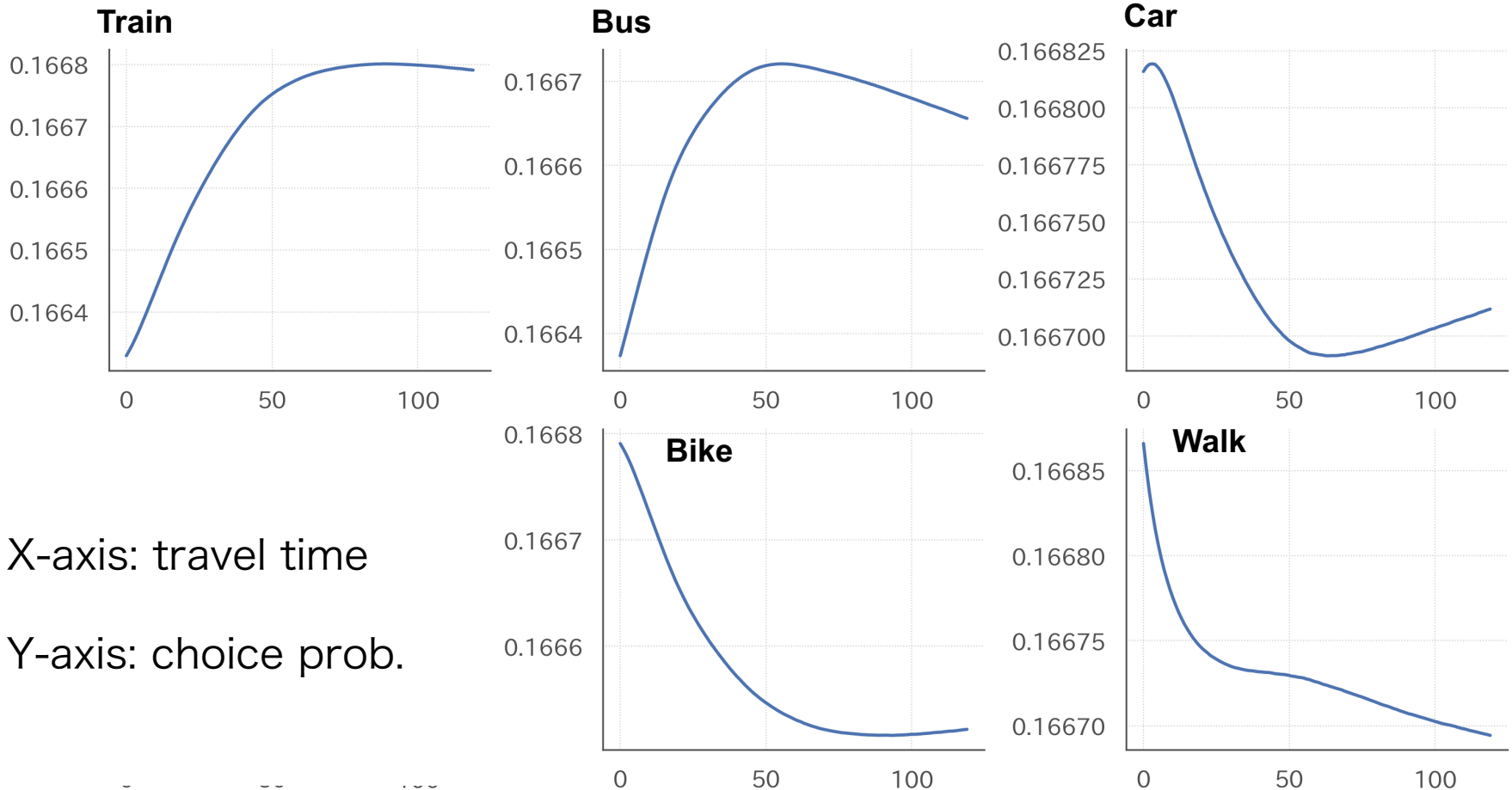
Results of PI (Permutation Importance)

- ◆ Calculating the **feature importance** in models.
- ◆ Determining important features for improving model accuracy



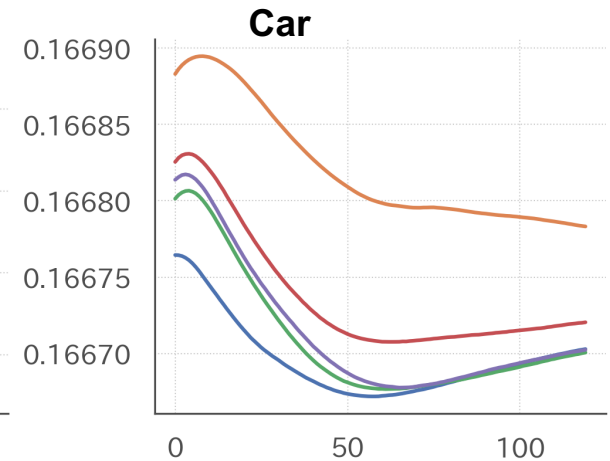
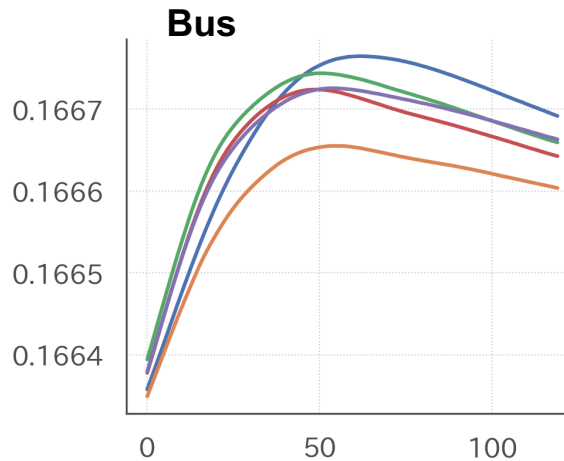
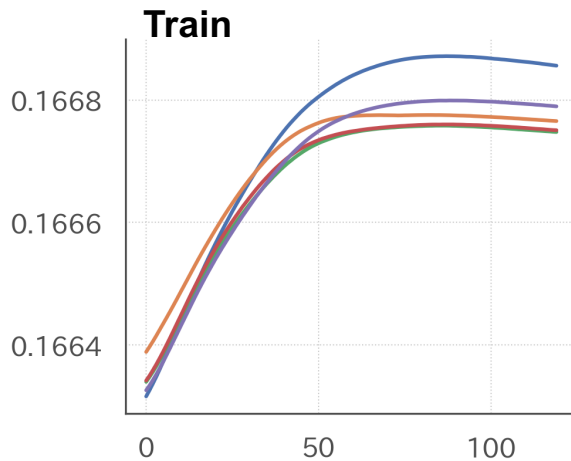
Results of PD(Partial Dependence)

- ◆ Calculating the **relationship** between output and each feature.
- ◆ Change point can be detected by **expected sensitivity**



Results of CPD(Partial Dependence)

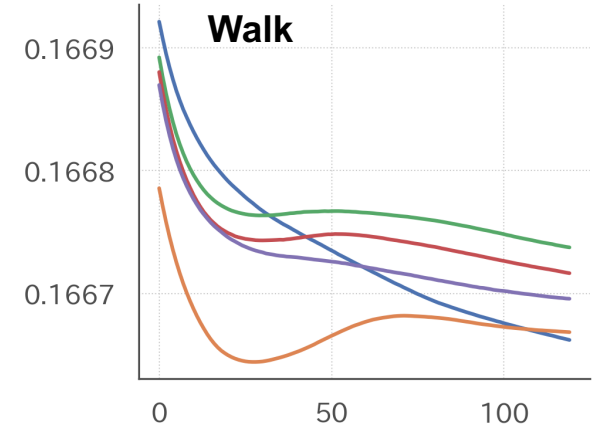
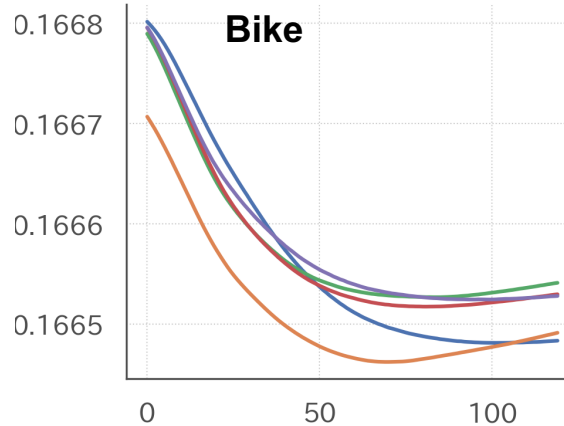
- ◆ Calculating the **relationship** between output and each feature.
- ◆ Change point can be detected by **group sensitivity**



X-axis: travel time

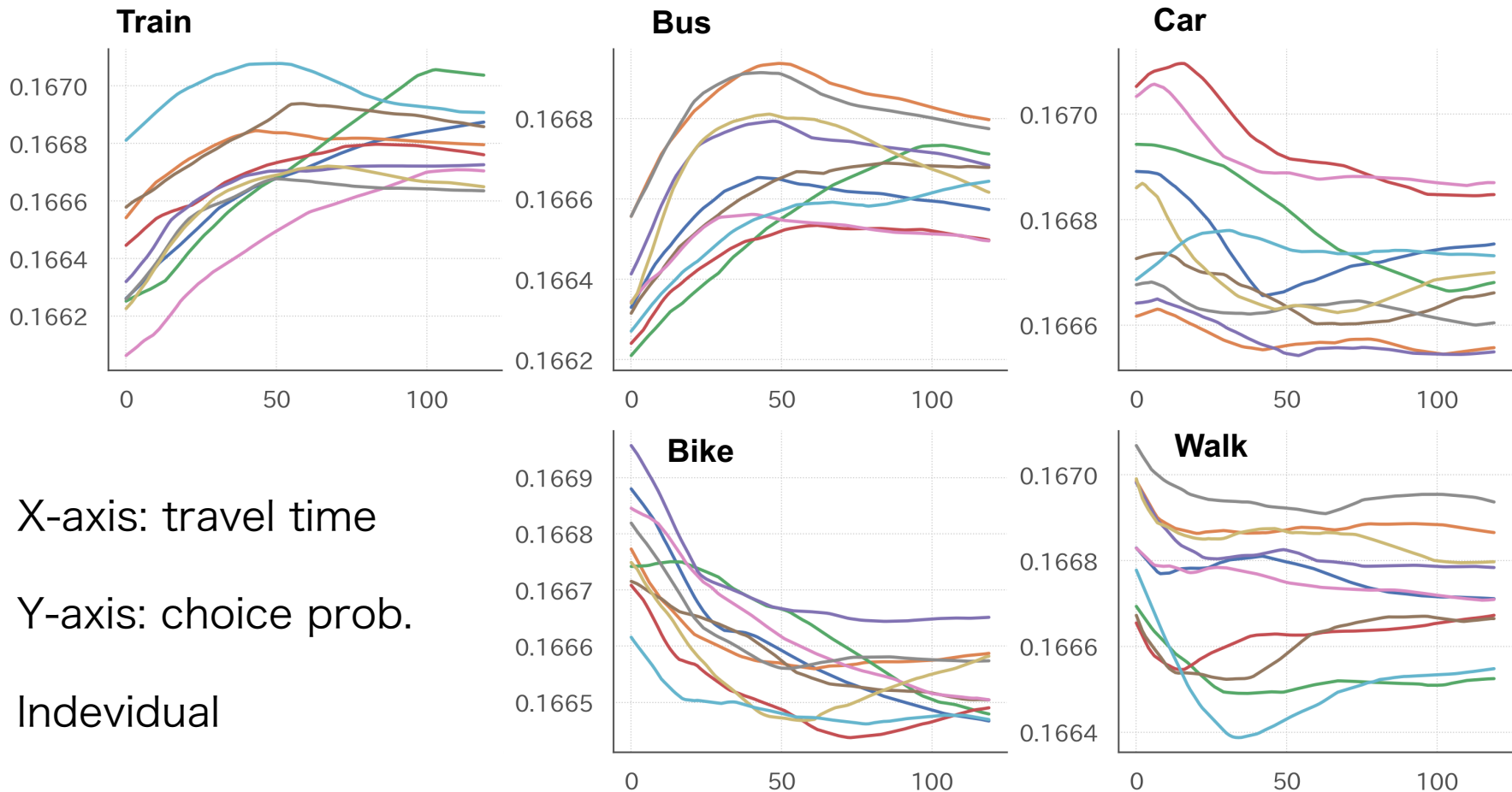
Y-axis: choice prob.

Travel Purpose



Results of ICE(Individual Conditional Expectation)

- ◆ Calculating the **relationship** between output and each feature.
- ◆ Change point can be detected by **individual sensitivity**



	DCM	ML
Explainability	<ul style="list-style-type: none">• Value of parameter and sign (+/-)• Elasticity• Sensitivity	<ul style="list-style-type: none">• Feature's importance• Feature's sensitivity• Degree of contribute• Group Heterogeneity• Individual parameter
Accuracy	<ul style="list-style-type: none">• Mid/Low (depend on N of alternatives)• Low calc. speed	<ul style="list-style-type: none">• High• High calc. speed
Methodological	<ul style="list-style-type: none">• RUM	<ul style="list-style-type: none">• Data driven

- ◆ XAI methods are powerful tools for more deep understanding for DCM.
 - Especially, model in-dependent methods (PFI, PD, SHAP) is good for us such as specification of utility function !
- ◆ Use different models depending on the situation.
 - DCM: Policy making, Explanation to citizen's etc.
 - ML: Monitoring, short-term forecasting, service design etc.

Thank you for your attention !

